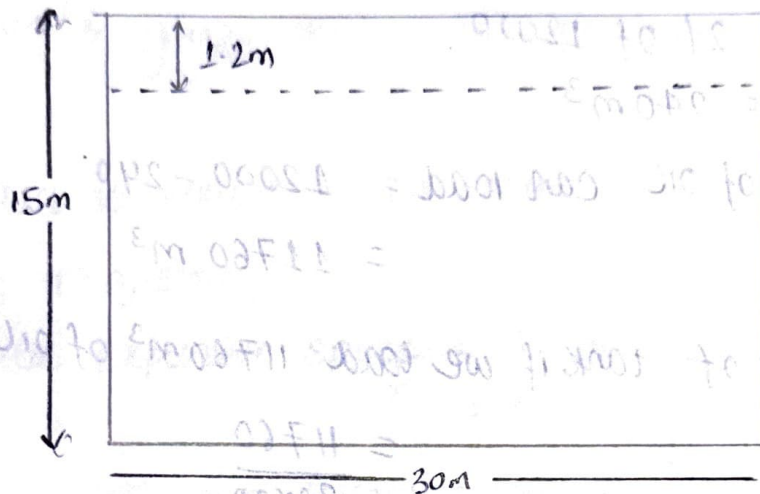


M-V HINDSHIP

(124)

A vessel at even keel has a tank of dimensions $30\text{m} \times 20\text{m} \times 15\text{m}$ deep containing crude oil of R.D 0.8345 at an ullage of 1.2m . Calculate the quantity of oil in the tank.

Soln:-



$$\text{Height of tank, } H = 15.0\text{m}$$

$$\text{Ullage, } U = 1.2\text{m}$$

$$\begin{aligned} \text{Sounding, } S &= H - U \\ &= 15.0 - 1.2 \\ &= 13.8\text{m} \end{aligned}$$

$$\begin{aligned} \text{Volume of oil in tank} &= L \times B \times \text{sounding} \\ &= 30 \times 20 \times 13.8 \\ &= 8280\text{m}^3 \end{aligned}$$

$$\begin{aligned} \text{Quantity of oil in MT} &= \text{Volume} \times \text{R.D} \\ &= 8280 \times 0.8345 \\ &= 6909.7\text{ M.T} \end{aligned}$$

(125)

An oil tanker has a tank of dimensions $30\text{m} \times 20\text{m} \times 20\text{m}$ deep and is loading oil at 38°C . It is desired to leave **2% of the volume of tank** for expansion. Calculate the quantity of oil and final ullage assuming that the vessel is at an even keel on completion. Given that R.D of oil at $25^\circ\text{C} = 0.8540$. Co-efficient of volume expansion = $0.0006/^\circ\text{C}$

Soln:-

$$\text{Volume of tank} = 30 \times 20 \times 20 \\ = 12000 \text{ m}^3$$

2% of volume of tank i.e. to leave for expansion

$$\begin{aligned} & 2\% \text{ of } 12000 \\ & = 240 \text{ m}^3 \end{aligned}$$

$$\begin{aligned} \text{So, volume of oil can load} &= 12000 - 240 \\ &= 11760 \text{ m}^3 \end{aligned}$$

Sounding of tank if we load 11760 m^3 of oil

$$= \frac{11760}{30 \times 20}$$

$$= 19.6 \text{ m}$$

Ullage = Height of tank - Sounding

$$\text{Ullage} = 20.0 - 19.6$$

$$\boxed{\text{Ullage} = 0.4 \text{ m}} \text{ Ans.}$$

Since, given RD is at 25°C & we are loading at 38°C
So, to get RD at 38°C

$$\text{coefficient} = 0.0006/^\circ\text{C}$$

$$\begin{aligned} \text{For } 25^\circ \text{ to } 38^\circ \text{ i.e. } 13^\circ \text{ change} &= 0.0006 \times 13 \\ &= 0.008 \end{aligned}$$

$$\begin{aligned} \text{Hence, RD of oil at } 38^\circ\text{C} &= 0.8540 - 0.008 \\ &= 0.8462 \end{aligned}$$

$$\text{Quantity of oil} = \text{volume of oil} \times \text{R.D.}$$

$$= 11760 \times 0.8462$$

$$= \boxed{9951.312 \text{ MT}} \text{ Ans}$$

- 126) A tank of dimension $20\text{m} \times 15\text{m} \times 10\text{m}$ is being loaded with an oil at 30°C (RD at $20^\circ\text{C} = 0.8681$). It is desired to leave 3% of volume of oil for expansion. Calculate the usage oil & quantity of oil loaded, given that coefficient of voluminous expansion $0.0005/^\circ\text{C}$

Let us assume volume of oil loaded at $30^\circ\text{C} = V$

According to question,

$$\text{Required expansion space} = 3\% \text{ of } V \\ = 0.03V$$

At any temperature following applies,

Volume of expansion space at 30°C + observed volume at $30^\circ\text{C} =$
Tank volume

$$(0.03V) + V = L \times B \times H$$

$$1.03V = 20 \times 15 \times 10$$

$$1.03V = 3000$$

$$V = 2912.621 \text{ m}^3 \text{ at } 30^\circ\text{C}$$

At given RD at $20^\circ\text{C} = 0.8681$

$$\text{Corrn to bring at } 30^\circ\text{C} = 0.0005 \times 10 \\ = 0.005 \text{ t/m}^3$$

$$\text{Density at } 30^\circ\text{C} = 0.8681 - 0.005 \quad \text{temp } \uparrow, \text{ density } \downarrow \\ = 0.8631 \text{ t/m}^3$$

$$\text{MT of oil loaded} = \text{vol @ } 30^\circ\text{C} \times \text{density @ } 30^\circ\text{C} \\ = 2912.621 \times 0.8631 \\ = \boxed{2513.88 \text{ t}}$$

$$\text{Sounding at } 30^\circ\text{C} = \frac{\text{Obs. vol @ } 30^\circ\text{C}}{L \times B}$$

$$= \frac{2912.621}{20 \times 15}$$

$$= 9.709 \text{ m}$$

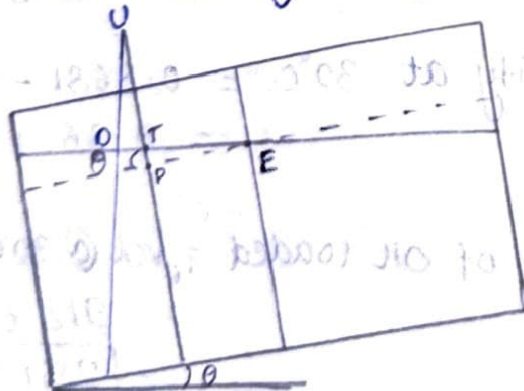
Hence, ullage at 30°C = Height - sounding

$$= 10 - 9.709$$

$$= \boxed{0.29 \text{ m}}$$

- 127) A crude oil tanker of LBP 250m has a tank of dimensions $30 \times 20 \times 20$ and is trimmed $\odot$ 3m by stern. The ullage port is in line with aft bulkhead and its height is 1.2m above the deck. The ullage of cargo as measured from ullage port is 2.2m using a sonic tape. Calculate the net observed volume/standard volume of oil & quantity of oil in MT loaded. Given density @ 15°C = 0.8550 and the loading temp is 31°C

Note:- According to the question, the ullage port is extending 1.2m above the deck & is in line with aft bulkhead. Since, the ullage port is in line with aft bulkhead, the sonic tape entering the tank space will slide along the aft bulkhead (since the vsl is trimmed by stern)



OO : observed ullage

UT : observed ullage after tape correction

In ΔUOT , (Tape correction)

$$\cos \theta = \frac{\text{Base}}{\text{hyp.}}$$

$$\cos \theta = \frac{UO}{UT}$$

$$UT = \frac{UO}{\cos \theta}$$

{ In vertical Δ , $\cos$
In horizontal Δ , $\tan$ }

In ΔPTE , (Trim correction)

$$\tan \theta = \frac{\text{perpendicular}}{\text{base}}$$

$$\tan \theta = \frac{PT}{PE}$$

Since $\tan \theta$ is equal to $\frac{\text{TRIM}}{\text{LBP}}$

$$\frac{\text{TRIM}}{\text{LBP}} = \frac{PT}{PE}$$

$PT \rightarrow$ trim correction

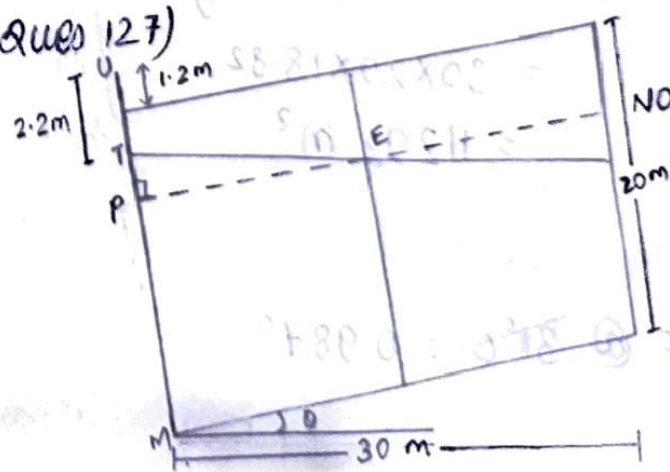
$$PE = \frac{l}{2} - d$$

where d is distance of ullage port from aft bulkhead
 l is length of tank

$$PE = \frac{10.50}{2} - 1.2$$

$$= 12.5m$$

Solution of Ques 127)



Note:- NO Tape correction is required as ullage port is in line with aft bulkhead

$$PE = \frac{l - d}{2}$$

$$= \frac{30}{2} - 0$$

$$= 15$$

$$* \frac{TRIM}{LBP} = \frac{PT}{PE}$$

$$\frac{3}{250} = \frac{PT}{15}$$

$$250 PT = 45$$

$$PT = \frac{45}{250}$$

$$PT = 0.18m$$

$$\text{Corrected range, } UP = UT + PT$$

$$= 2.2 + 0.18$$

$$= 2.38m$$

$$\text{Sounding @ } 31^{\circ}C_{PM} = \text{Reference height}_{UM} - \text{range}_{UP}$$

$$= (20 + 1.2) - 2.38$$

$$= 21.2 - 2.38$$

$$= 18.82m$$

$$\text{Obs. vol. @ } 31^{\circ}C = L \times B \times \text{sounding @ } 31^{\circ}C$$

$$= 30 \times 20 \times 18.82$$

$$= 11292 m^3$$

Against temp $31^{\circ}C$ & density 0.8550, in ASTM Table 54A

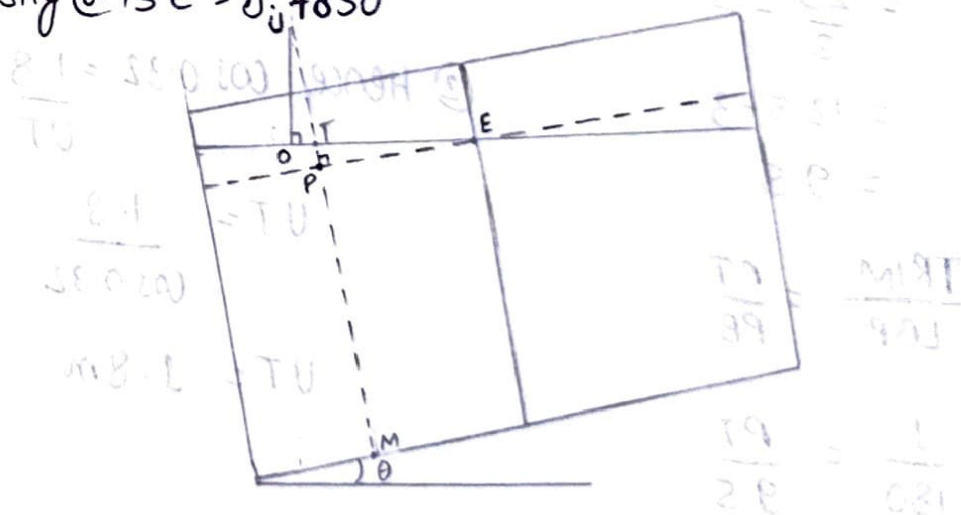
$$VCF @ 31^{\circ}C = 0.9873$$

$$\begin{aligned}\text{Standard volume @ } 15^{\circ}\text{C} &= \text{obs. vol. @ } 31^{\circ}\text{C} \times \text{VCF @ } 31^{\circ}\text{C} \\ (\text{N.O.V}) &= 11292 \times 0.9873 \\ &= \boxed{11148.592 \text{ m}^3} @ 15^{\circ}\text{C}\end{aligned}$$

$$\begin{aligned}\text{WCF/WRF/density in air @ } 15^{\circ}\text{C} &= \text{density in vacuum} - 0.0011 \\ &= 0.8550 - 0.0011 \\ &= 0.8539 \text{ t/m}^3\end{aligned}$$

$$\begin{aligned}\text{Quantity loaded in MT} &= \text{Std vol. @ } 15^{\circ}\text{C} \times \text{density in air @ } 15^{\circ}\text{C} \\ &= 11148.592 \times 0.8539 \\ &= \boxed{9519.78 \text{ MT}}\end{aligned}$$

- 128) An oil tanker of LBP 180m is loading oil at 35°C in one of her tanks of dimension $25 \times 20 \times 18$. On completion of loading vessel is trimmed 1m by stern and ullage of the cargo in tank was observed to be 1.8m using a sonic tape. The ullage port is located 3m fwd of aft bulkhead & 1m above the deck. Calⁿ the net obs. vol. of oil in tank. Density @ $15^{\circ}\text{C} = 0.7850$



Note:- If the ullage port is located aft of the centerline & the vessel is trimmed by stern, then in that case the trim correction will be positive. i.e. PT will be added to UT. And in case, vessel is down by head, then trim correction will be negative, PT will be subtracted from UT

When vessel's trim ^{by aft} & posⁿ of ullage port is in aft of CL, the correction is positive. (v.o.u)

When vessel is down by head & posⁿ of ullage port is in fwd of CL, the correction is positive

When vessel trim by stern, & posⁿ of ullage is in fwd of CL, the trim correction is negative

When vessel is down by head & posⁿ of ullage port is in aft of CL, the correction is negative

Solⁿ of 128 M.V. Hindship, 28/11/11

④ In ΔPTE (trim corrⁿ) ② In ΔUOT (Tape corrⁿ)

$$\tan \theta = \frac{PT}{PE}$$

$$\cos \theta = \frac{UO}{UT}$$

$$\frac{TRIM}{LBP} = \frac{PT}{PE}$$

$$\textcircled{1} \tan \theta = \frac{TRIM}{LBP}$$

$$\textcircled{3} \text{ For PE, } \frac{1}{2} - d$$

$$\tan \theta = \frac{1}{180}$$

$$= \frac{25 - 3}{2}$$

$$\theta = 0.32^\circ$$

$$= 12.5 - 3$$

$$\textcircled{2} \text{ Hence, } \cos 0.32^\circ = \frac{1.8}{UT}$$

$$= 9.5$$

$$UT = \frac{1.8}{\cos 0.32^\circ}$$

$$\textcircled{4} \frac{TRIM}{LBP} = \frac{PT}{PE}$$

$$UT = 1.8 \text{ m}$$

$$\frac{1}{180} = \frac{PT}{9.5}$$

$$180 PT = 9.5$$

$$PT = \frac{9.5}{180}$$

$$PT = 0.053 \text{ m}$$

$$\textcircled{5} \text{ corrected ullage, } UP = UT + PT$$

$$= 1.8 + 0.053$$

$$= 1.853 \text{ m}$$

$$\text{Sounding @ } 35^{\circ}\text{C} = \text{Ref. height} - \text{corrected ullage}$$

$$= (18+1) - 1.853$$

$$= 19 - 1.853$$

$$= 17.147 \text{ m}$$

$$\text{Gross observed volume @ } 35^{\circ}\text{C} = L \times B \times \text{sounding @ } 35^{\circ}\text{C}$$

$$= 25 \times 20 \times 17.147$$

$$= 8573.61 \text{ m}^3$$

Against density 0.7850 & temp 35°C , From ASTM TABLE 54

$$\text{VCF @ } 35^{\circ}\text{C} = 0.9809$$

$$\text{Gross standard volume @ } 15^{\circ}\text{C} = \underset{\substack{\text{OR} \\ \text{N.O.V}}}{GSOV @ 35^{\circ}\text{C}} \times \text{VCF @ } 35^{\circ}\text{C}$$

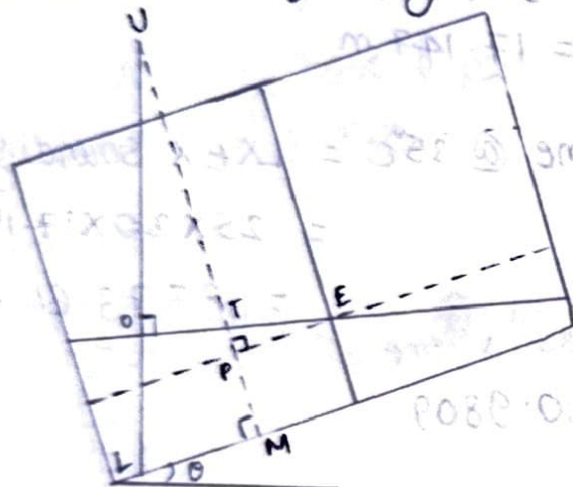
$$= 8573.61 \times 0.9809$$

$$= \boxed{8409.855 \text{ m}^3}$$

129) H.W for revision

130) while discharging oil from an oil tanker of LBP 175m, sounding of a tank was obtained as 800m using a sounding rod. The dimension of the tank are 20X15X15m. The vessel was trimmed 1.5m by stern and the sounding pipe is located 3m from aft bulkhead & extends 1.0m above deck. Assuming no wedge formed, calculate the quantity of oil in the tank. ~~density of oil = 0.8500 t/m³~~

Soln:-



temp. of oil cargo = 30°C

$$\textcircled{1} \quad \tan \theta = \frac{\text{TRIM}}{\text{LBP}}$$

$$\tan \theta = \frac{1.5}{175}$$

$$\theta = 0.49^\circ$$

~~② In AVOI (TOP CORR)~~

$$\cos \theta = \frac{VO}{VT}$$

$$\cos \theta = 0.8$$

$$\cos 0.49^\circ = \frac{0.8}{VT}$$

$$VT = \frac{0.8}{\cos 0.49^\circ}$$

$$VT = 0.8005 \text{ m}$$

$$UM = \text{Ref. height} + \text{Height of tank}$$

$$= 1.0 + 15.0$$

$$= 16.0 \text{ m}$$

$$PE = \frac{l}{2} - d$$

$$= \frac{20}{2} - 3$$

$$= 7 \text{ m}$$

In ΔULM ,

$$\cos \theta = \frac{\text{Base}}{\text{Hyp}} = \frac{UM}{UL}$$

$$\cos 0.49^\circ = \frac{16.0}{UL}$$

$$UL = 16.000$$

$$UL = UO + OL$$

$$16 = UO + 0.8$$

$$UO = 15.20m$$

In ΔUOT (Tape corrⁿ)

$$\cos \theta = \frac{UO}{UT}$$

$$\cos 0.49^\circ = \frac{15.20}{UT}$$

$$UT = \frac{15.20}{\cos 0.49^\circ}$$
$$= 15.200m$$

In ΔPTE (Trim corrⁿ)

$$\tan \theta = \frac{PT}{PE}$$

$$\frac{\text{TRIM}}{\text{LBP}} = \frac{PT}{PE}$$

$$\frac{1.5}{175} = \frac{PT}{7}$$

$$10.5 = 175 PT$$

$$PT = 0.06m$$

$$UP = UT + PT$$

$$= 15.20 + 0.06$$

$$= 15.26m$$

$$PM \text{ i.e. sounding @ sec} = (\text{Ref height} + \text{Height of tank}) - UP$$
$$= 16 - 15.26$$
$$= 0.74m$$

~~Volume of tank~~

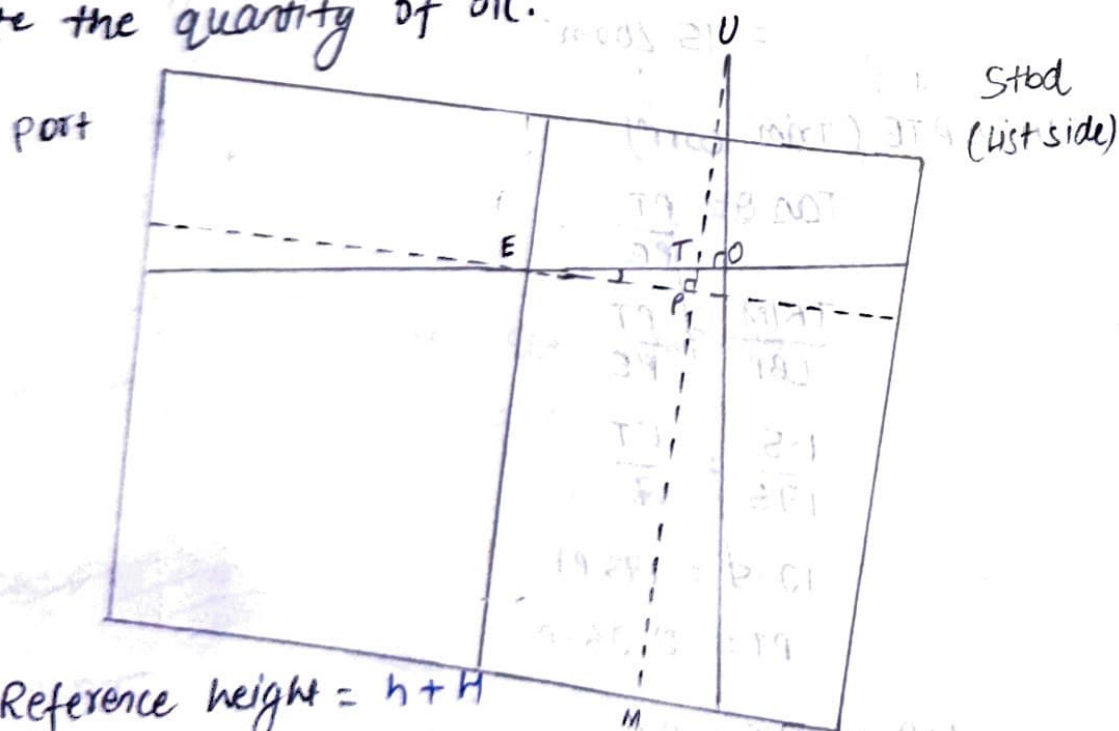
Gross observed volume @ 32°C = $L \times B \times \text{sounding @ } 30^{\circ}\text{C}$
 ROB
 $= 20 \times 15 \times 0.74$
 $= 222 \text{ m}^3$

~~ref @ 32°C~~

Note:- Use term ROB in case of discharging & have very less sounding.

(131)

A vessel of LBP 235m has a tank of dimension $30 \times 25 \times 20$ is loading oil of density @ 15°C : 0.8150. On completion of loading vessel is listed 1° stbd and the ullage is observed using a sonic tape was found to be 1.8m. Ullage port is located 3m to stbd of CL & 1m above deck. Vessel is on an keel on completion and temp. of oil to observed to be 32°C . Calculate the quantity of oil.



Reference height = $h + H$
 $= 1 + 20$
 $= 21 \text{ m}$

$PE = d = 3 \text{ m}$

$\theta = 1^{\circ}$

In ΔUOT (tape corr)

$$\cos \theta = \frac{UO}{UT}$$

$$\cos 1^\circ = \frac{1.8}{UT}$$

$$UT = 1.800 \text{ m}$$

In ΔPTE (vist corr)

$$\tan \theta = \frac{PT}{PE}$$

$$\tan 1^\circ = \frac{PT}{3}$$

$$PT = 3 \times \tan 1^\circ \\ = 0.052 \text{ m}$$

Corrected ullage, $UP = UT + PT$

$$= 1.8 + 0.052$$

$$= 1.852 \text{ m}$$

Corrected sounding @ 32°C = Reference height - ullage

$$= 21 - 1.852$$

$$= 19.148 \text{ m}$$

Gross observed volume @ 32°C = $L \times B \times \text{corr'd sounding @ } 32^\circ\text{C}$

$$= 30 \times 25 \times 19.148$$

$$= 14361.0 \text{ m}^3$$

$$VCF @ 32^\circ\text{C} = 0.9852$$

Gross standard volume @ 15°C = 14361×0.9852

$$= 14148.4572 \text{ m}^3$$

WCF/WRF/ density in air @ 15°C = density in vac. - 0.0011

$$= 0.8150 - 0.0011$$

$$= 0.8139 \text{ t/m}^3$$

Quantity loaded in MT = $GSV @ 15^\circ\text{C} \times \text{density in air @ } 15^\circ\text{C}$

$$= 14148.4572 \times 0.8139$$

$$= 11515.429 \text{ MT}$$

(132)

On completion of cargo, at time of sounding the tank, dip was observed to be 9cm. The vessel was upright & trimmed 3m by stern. Dimensions of the tank were 36m x 27m x 18m. LBP of the vessel was 270m. Calculate the on-board quantity (OBQ) given that the sounding pipe was located 5m from aft bulkhead and 0.9m above deck.



$$\tan \theta = \frac{\text{TRIM}}{\text{LBP}} = \frac{3}{270} = 0.011^\circ$$

$$\theta = 0.64^\circ$$

$$UM = h + 4$$

$$= 0.9 + 18$$

$$= 18.9$$

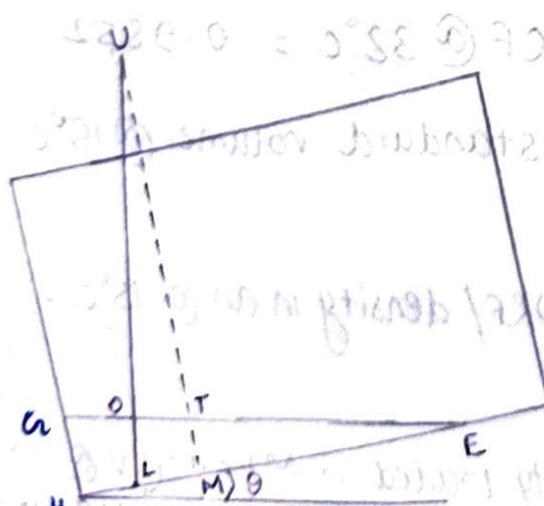
Note:- Dip of 9cm means wedge is forming

$$PE = \frac{L}{2} = d$$

$$= \frac{36}{2} = 18$$

$$= 18.5$$

$$= 13$$



In $\triangle ULM$, $\angle M = 90^\circ$

$$\cos \theta = \frac{UM}{UL}$$

$$\cos 0.64^\circ = \frac{18.9}{UL}$$

$$UL = \frac{18.9}{\cos 0.64^\circ}$$

$$UL = 18.901 \text{ m}$$

$$UL = UO + OL$$

$$18.901 = UO + 0.09$$

$$UO = 18.901 - 0.09 \\ = 18.811 \text{ m}$$

In $\triangle UOT$ (Tape triangle), $\angle O = 90^\circ$

$$\cos \theta = \frac{UO}{UT}$$

$$\cos 0.64^\circ = \frac{18.811}{UT}$$

$$UT = \frac{18.811}{\cos 0.64^\circ}$$

$$UT = 18.812 \text{ m}$$

$$UM = UT + TM$$

$$18.9 = 18.812 + TM$$

$$TM = 18.9 - 18.812$$

$$= 0.088 \text{ m}$$

In $\triangle TME$ (Trim triangle), $\angle M = 90^\circ$

$$\tan \theta = \frac{TM}{EM} \Rightarrow \frac{\text{TRIM}}{\text{LBP}} = \frac{TM}{EM}$$

$$\tan 0.64^\circ = \frac{0.088}{EM} \Rightarrow \frac{3}{270} = \frac{0.088}{EM}$$

$$EM = \frac{0.088 \times 270}{3}$$

$$EM = 7.920 \text{ m}$$

$$HE = HM + EM$$

$$HE = 5 + \cancel{7.878} 7.920$$

$$\cancel{12.878} = 12.920$$

$$\therefore HE < L$$

HE is less than length of tank

$\therefore$ wedge is confirmed

$$\text{In } \triangle GHE, \angle H = 90^\circ$$

$$\tan \theta = \frac{GH}{HE}$$

$$\frac{\text{TRIM}}{\text{LBP}} = \frac{GH}{HE}$$

$$\frac{3}{270} = \frac{GH}{12.920}$$

$$270 GH = 3876$$

$$GH = 0.144$$

$$\text{Area of } \triangle GHE = \frac{1}{2} \times HE \times GH \left(\frac{1}{2} \times \text{base} \times \text{height} \right)$$

$$= \frac{1}{2} \times \cancel{12.878} 12.920 \times 0.144$$

$$\cancel{0.930} = 0.930$$

$$\text{Volume of ROB} = \frac{\text{Area of } \triangle GHE \times \text{breadth}}{\text{AGHE}}$$

$$= 0.930 \times 27$$

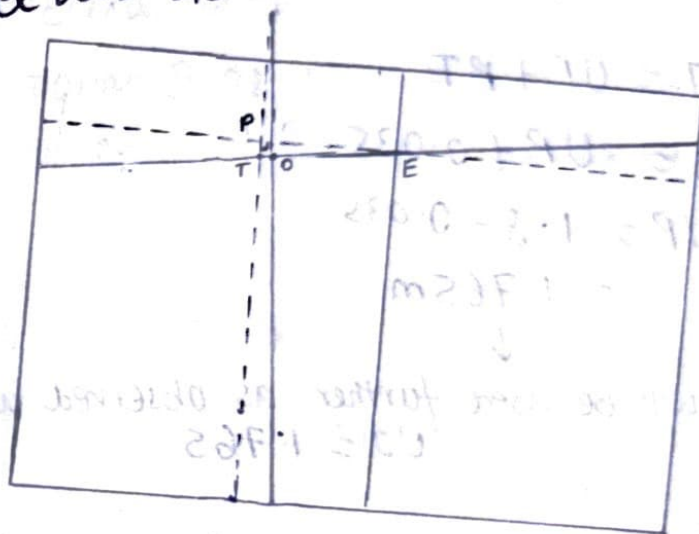
$$= 25.116 \text{ m}^3$$

133

A box shaped tank 30X18X20 containing crude oil of dens at $15^{\circ}\text{C} = 0.8275 \text{ t/m}^3$ had an ullage of 1.80m as measured by sonic tape. The ullage port was located 3m fwd of aft bulkhead, 1m above the tank top and 2m to port of CL tank. Trim observed was 3m & vessel listed 1° to starboard. Obs. temp: 32.5°C . Calculate the qty of oil in tank if the LBP of vessel was 215m

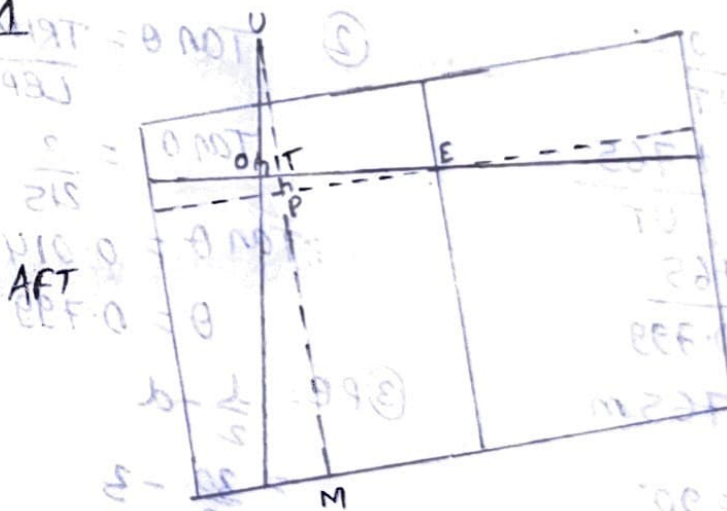
LIST

PORT



STBD
(LIST)

TRIM



FWD

First List

In ΔUOT , $\angle O = 90^{\circ}$

$$\cos \theta = \frac{UO}{UT}$$

$$\cos 1^{\circ} = \frac{1.8}{UT}$$

$$UT = 1.800 \text{ m}$$

$$\frac{T9}{31} = \frac{MRT}{105}$$

$$\frac{T9}{31} = \frac{3}{215}$$

$$\frac{T9}{31} = \frac{3}{215}$$

$$T9 = 3.1 \text{ m}$$

In ΔPTE , $\angle P = 90^\circ$

$$\tan \theta = \frac{PT}{PE}$$

$$\tan 1^\circ = \frac{PT}{2} \rightarrow \text{bcz dist from CL}$$

$$PT = 2 \times \tan 1^\circ$$
$$= 0.035 \text{ m}$$

$$UT = UP + PT$$

$$1.8 = UP + 0.035$$

$$UP = 1.8 - 0.035$$
$$= 1.765 \text{ m}$$

↓

This will be used further as observed draught in Trim A

$$UP = UO = 1.765$$

Second trim

In ΔUOT , $\angle O = 90^\circ$

$$\cos \theta = \frac{UO}{UT}$$

$$\cos 0.799^\circ = \frac{1.765}{UT}$$

$$UT = \frac{1.765}{\cos 0.799^\circ}$$

$$UT = 1.765 \text{ m}$$

In ΔPTE , $\angle P = 90^\circ$

$$\tan \theta = \frac{PT}{PE}$$

$$\frac{\text{TRIM}}{\text{LBP}} = \frac{PT}{PE}$$

$$\frac{3}{245} = \frac{PT}{12}$$

$$PT = 0.167$$

$$\textcircled{1} UM = H + h = 20 + 1 = 21 \text{ m}$$

$$\textcircled{2} \tan \theta = \frac{\text{TRIM}}{\text{LBP}}$$

$$\tan \theta = \frac{3}{245}$$

$$\tan \theta = 0.014$$

$$\theta = 0.799^\circ$$

$$\textcircled{3} PE = \frac{L}{2} - d$$

$$= \frac{30}{2} - 3$$

$$= 15 - 3$$

$$= 12$$

$$UP = UT + PT$$

$$UP = 0000 1.765 + 0.167$$

$$= 1.932$$

$$UM = UP + PM$$

$$21 = 1.932 + PM$$

$$PM = 21 - 1.932 = 19.068m$$

Therefore, corrected sounding @ 32.5°C (PM) = 19.068m

$$\text{Observed volume @ 32.5°C} = \bullet LX B \times \text{corr'd sounding @ 32.5°C}$$

$$= 30 \times 18 \times 19.068$$

$$= 10296.72m^3$$

$$VCF @ 32.5°C = 0.9852$$

$$\text{Standard volume @ 15°C} = \text{Obs. vol. @ 32.5°C} \times VCF @ 32.5°C$$

$$= 10296.72 \times 0.9852$$

$$= 10144.329m^3$$

$$WCF/WRF/\text{density in air @ 15°C} = \text{density in vac} - 0.0011$$

$$= 0.8275 - 0.0011$$

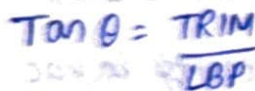
$$= 0.8264 \text{ t/m}^3$$

$$\text{Quantity loaded in MT} = \text{NSV @ 15°C} \times \text{density in air @ 15°C}$$

$$= 10144.329 \times 0.8264 \text{ t}$$

$$= 8383.273 \text{ MT}$$

An oil tanker of LBP 200m has a box shaped tank of dimensions $40 \times 20 \times 20$ and is loaded with oil. On completion ullage as measured from sonic tape was observed to be 1.24m and temp was 37°C . A water dip ullage of 20.94m was also found. The ullage port was located 1.1m above the tank top and 1.6m fwd of aft bulkhead. Vessel was trimmed 3m by stern. Terminal gave the density of oil @ 15°C as 0.8145 t/m^3 . Determine the quantity of oil in tank.



$$\theta = 0.86^\circ$$

$$= \frac{40}{2} - 1.6$$

$$= 20 - 1.6$$

$$= T_M = 18.4$$

$$\cos \theta = \frac{v_D}{v_T}$$

$$\cos 0.86^\circ = \frac{1.24}{UT}$$

$$UT = \frac{1.24}{\cos 0.86^\circ}$$

$$UT = 1.240 \text{ m}$$

$$\tan \theta = \frac{PT}{PE}$$

$$\frac{\text{TRIM}}{\text{LBP}} = \frac{\text{PT}}{\text{PE}}$$

$$\frac{3}{200} = \frac{\text{PT}}{18.4}$$

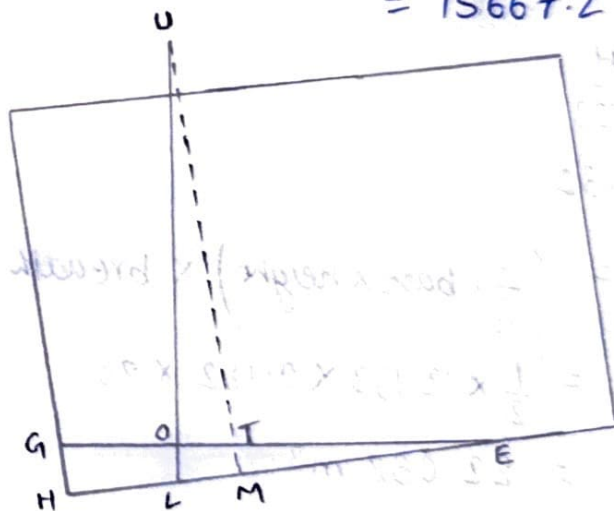
$$\text{PT} = 0.276$$

$$\begin{aligned}\text{Corrected ullage, } UP &= UT + PT \\ &= 1.240 + 0.276 \\ &= 1.516\end{aligned}$$

$$UM = UP + PM$$

$$\begin{aligned}\text{Sounding, } PM &= UM - UP \\ &= (20 + 1.1) - 1.516 \\ &= 21.1 - 1.516 \\ &= 19.584\end{aligned}$$

$$\begin{aligned}\text{Volume of oil in tank} &= L \times B \times \text{sounding} \\ &= 40 \times 20 \times 19.584 \\ &= 15667.2 \text{ m}^3\end{aligned}$$



In ΔUOT

$$\cos \theta = \frac{UT}{UP}$$

$$\cos 0.86^\circ = \frac{20.94}{UP}$$

$$UP = 20.942 \text{ m}$$

$$UM = UT + TM$$

$$TM = UM - UT$$

$$TM = (20 + 1.1) - 20.942$$

$$TM = 21.1 - 20.942$$

$$TM = 0.158m$$

In $\triangle TME$,

$$\tan \theta = \frac{TM}{ME}$$

$$\frac{3}{200} = \frac{0.158}{ME}$$

$$ME = 10.533m$$

$$HE = HM + ME$$

$$HE = 1.6 + 10.533$$

$$HE = 12.133m$$

In $\triangle GHE$,

$$\tan \theta = \frac{GH}{HE}$$

$$\frac{3}{200} = \frac{GH}{12.133}$$

$$GH = 0.182$$

$$\begin{aligned} \text{Volume of } \triangle GHE &= \left(\frac{1}{2} \times \text{base} \times \text{height} \right) \times \text{breadth} \\ &= \frac{1}{2} \times 12.133 \times 0.182 \times 20 \\ &= 22.082 m^3 \end{aligned}$$

$$\begin{aligned} \text{Volume of oil in tank} &= \text{Total volume} - \text{vol. of water} \\ &= 15667.2 - 22.082 \end{aligned}$$

$$G.O.V. @ 37^\circ C = 15645.118 m^3$$

$$(0.8145) VCF @ 37^\circ C = 0.9808$$

$$\begin{aligned}\text{Gross standard volume} &= G.O.V @ 37^{\circ}\text{C} \times VCF @ 37^{\circ}\text{C} \\ &= 15645.118 \times 0.9808 \\ &= 15344.732 \text{ m}^3\end{aligned}$$

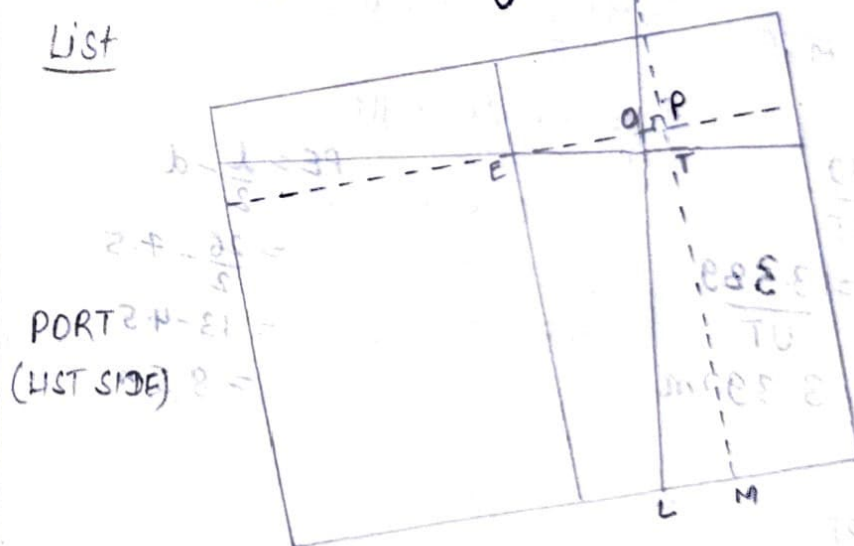
$$\begin{aligned}\text{WCF/WRF/density in air} &= \text{density in vacuum} - 0.0011 \\ &= 0.8145 - 0.0011 \\ &= 0.8134\end{aligned}$$

$$\begin{aligned}\text{Quantity of oil} &= G.S.V \times \text{density in air} \\ &= 15344.732 \times 0.8134 \\ &= 12481.4 \text{ M.T}\end{aligned}$$

PREVIOUS YEAR SOLN

A vessel of LBP 108m arrives discharge port with trim 2.0 by stern and 2° list to port. A box shaped cargo tank measure 26x16x9.3 has ullage of 3.52m by sonic tape, temp 42.3°C, noted from ullage port located 4.5m fwd of aft bulkhead, 3.8m to stbd of CL & 114 cm above the top of tank. On completion of cargo operation 26 cm dip was noted from same ullage port when the trim was 4m by stern with no list. Find the quantity of oil discharged & ROB. If oil density 8226.3 kg/cm³ in vacuum at 15°C

List



STBD

$$\begin{aligned}\tan \theta &= \frac{\text{TRIM}}{\text{LBP}} = \frac{2}{108} \\ \theta &= 1.06^{\circ}\end{aligned}$$

In ΔUOT , (List triangle)

$$\cos \theta = \frac{UO}{UT}$$

$$\cos 2.00^{\circ} = \frac{3.52}{UT}$$

$$UT = 3.52 \text{ m}$$

$$PE = 3.8 \text{ m}$$

In ΔPTE , $\tan \theta = \frac{PT}{PE}$

$\frac{\text{TRIM}}{\text{LBP}} = \frac{PT}{PE}$

$\tan(4.1^\circ) = \frac{PT}{PE}$

$\tan 2^\circ = \frac{PT}{3.8}$

$PT = 0.133m$

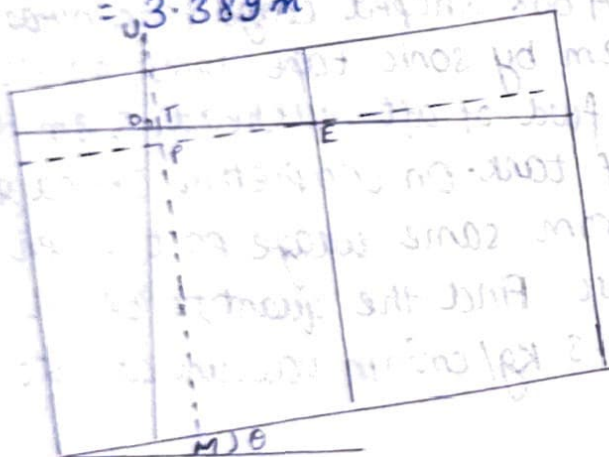
$\therefore UT = UP + PT$

$3.522 = UP + 0.133$

$UP = 3.522 - 0.133$

$= 3.389m$

* $UP = UD = 3.389$



In ΔUOT ,

$\cos \theta = \frac{UD}{UT}$

$\cos 1.06^\circ = \frac{3.389}{UT}$

$UT = 3.390m$

$PE = \frac{1}{2} - d$

$= \frac{26}{2} - 4.5$

$= 13 - 4.5$

$= 8.5m$

In ΔPTE ,

$\tan \theta = \frac{PT}{PE}$

$\frac{\text{TRIM}}{\text{LBP}} = \frac{PT}{8.5}$

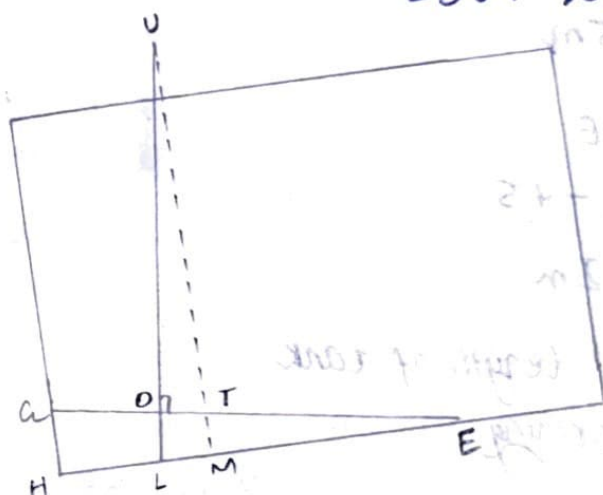
$\frac{2}{108} = \frac{PT}{8.5}$

$PT = 0.157m$

corrected
wedge, $UP = UT + PT$
 $= 3.390 + 0.157$
 $= 3.547$

80 $UM = UP + PM$
 $(9.3 + 1.14) = 3.547 + PM$
 $10.44 = 3.547 + PM$
 sounding, $PM = 6.893 \text{ m}$

Volume of oil in tank = $26 \times 16 \times 6.893$
 $= 2867.488 \text{ m}^3$



$\tan \theta = \frac{\text{TRIM}}{\text{LBP}} = \frac{4}{108}$
 $\theta = 2.121^\circ$

In $\triangle UML$, $\cos \theta = \frac{UM}{UL}$
 $\cos 2.121^\circ = \frac{10.44}{UL}$
 $UL = 10.447 \text{ m}$

$UL = UO + OL$
 $10.447 = UO + 0.26$
 $UO = 10.187 \text{ m}$

In $\triangle UOT$, $\cos \theta = \frac{UO}{UT}$
 $\cos 2.121^\circ = \frac{10.187}{UT}$
 $UT = 10.194 \text{ m}$

~~to find ME,~~

~~$\tan \theta = \frac{TM}{ME}$~~
 ~~$\frac{4}{108} = \frac{TM}{ME}$~~

$$UM = UT + TM$$

$$10.44 = 10.194 + TM$$

$$TM = 0.246m$$

In $\triangle TME$,

$$\tan \theta = \frac{TM}{ME}$$

$$\frac{4}{108} = \frac{0.246}{ME}$$

$$ME = 6.642m$$

$$HM = 4.5m$$

$$HE = HM + ME$$

$$= 6.642 + 4.5$$

$$= 11.142m$$

HE is less than length of tank
 $\therefore$ wedge is forming

In $\triangle GHE$,

$$\tan \theta = \frac{GH}{HE}$$

$$\frac{4}{108} = \frac{GH}{11.142}$$

$$GH = 0.413m$$

$$\text{Volume of oil in } \triangle GHE = \left(\frac{1}{2} \times \text{base} \times \text{height} \right) \times \text{breadth}$$

$$= \frac{1}{2} \times HE \times GH \times \text{breadth}$$

$$= \frac{1}{2} \times 11.142 \times 0.413 \times 16$$

$$= 36.813 m^3$$

$$\boxed{i.e. ROB = 36.813 m^3}$$

$$\text{Volume of oil discharged} = 2867.488 - 36.813$$

$$G.O.V @ 42.3^\circ C = 2830.675 \text{ m}^3$$

$$VCF @ 42.3^\circ C = 0.9768$$

$$G.S.V = 2830.675 \times 0.9768$$

$$= 2765.003 \text{ m}^3$$

$$WCF = 0.8226 - 0.0011$$

$$= 0.8215$$

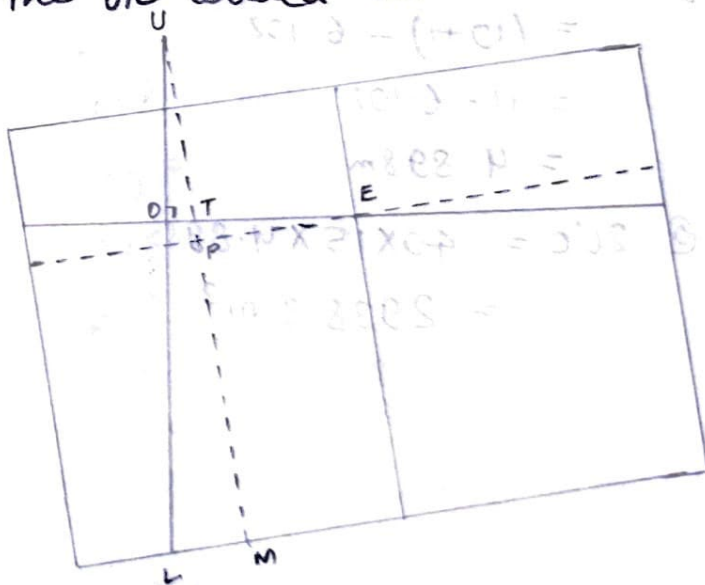
$$\text{Qty discharge} = G.S.V \times WCF$$

$$= 2765.003 \times 0.8215$$

$$= 2271.45 \text{ M.T}$$

Ques
March
2021

Using ASTM table, calculate the quantity of white oil in a rectangular tank of ship of LBP 130m, trimmed 1.5m by stern, dimension of the tank are 40m x 15m x 10m. The ullage port is located 1.0m above the deck, 2.5m from tank aft bulkhead and 2m to the port of CL. The ullage was taken by sonic tape & was measured as 5.9m & water cut of 10cm was obtained. The temp. of the oil loaded was 26°C. & density of oil at 15°C is 820 kg/m³.



$$\tan \theta = \frac{\text{TRIM}}{\text{LBP}}$$

$$\tan \theta = \frac{1.5}{130}$$

$$\theta = 0.66^\circ$$

$$PE = \frac{l}{2} - d$$

$$= \frac{40}{2} - 2.5$$

$$= 20 - 2.5$$

$$= 17.5 \text{ m}$$

In ΔUOT ,

$$\cos \theta = \frac{UO}{UT}$$

$$\cos 0.66^\circ = \frac{5.9}{UT}$$

$$UT = \frac{5.9}{\cos 0.66^\circ}$$

$$UT = 5.900m$$

In ΔPTE , $\tan \theta = \frac{PT}{PE}$

$$\frac{TRIM}{LBP} = \frac{PT}{PE}$$

$$\frac{1.5}{130} = \frac{PT}{17.5}$$

$$PT = 0.202m$$

$$UP = UT + PT$$

$$UP = 5.900 + 0.202$$

$$\text{Corrected ullage } UP = 6.102m$$

$$UM = UP + PM$$

$$\text{Sounding, } PM = UM - UP$$

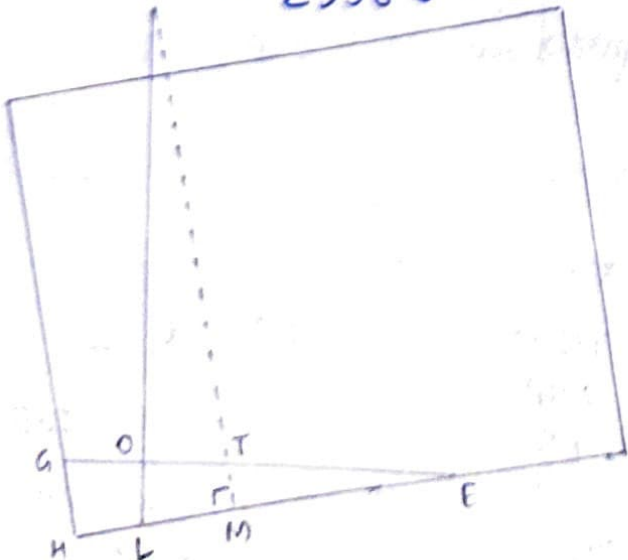
$$= (10+1) - 6.102$$

$$= 11 - 6.102$$

$$= 4.898m$$

$$T.O.V @ 26^\circ C = 40 \times 15 \times 4.898$$

$$V = 2938.8 m^3$$



T.O.V includes free water

In ΔULM ,

$$\cos \theta = \frac{UM}{UL}$$

$$\cos 0.66^\circ = \frac{11}{UL}$$

$$UL = 11.000 \text{ m}$$

$$UL = UO + OL$$

$$11.000 = UO + 0.10$$

$$UO = 10.90 \text{ m}$$

In ΔUOT ,

$$\cos \theta = \frac{UO}{UT}$$

$$\cos 0.66^\circ = \frac{10.90}{UT}$$

$$UT = 10.900 \text{ m}$$

$$UM = UT + TM$$

$$11 = 10.900 + TM$$

$$TM = 0.10 \text{ m}$$

In ΔTME ,

$$\tan \theta = \frac{TM}{ME}$$

$$\frac{TRIM}{LBP} = \frac{TM}{ME}$$

$$\frac{1.5}{130} = \frac{0.10}{ME}$$

$$ME = 8.667 \text{ m}$$

$$HE = HM + ME$$

$$= 2.5 + 8.667$$

$$= 11.167 \text{ m}$$

HE is less than L, wedge is confirmed.

In ΔGHE ,

$$\tan \theta = \frac{GH}{HE}$$

$$\frac{1.5}{130} = \frac{GH}{11.167}$$

$$GH = 0.129 \text{ m}$$

$$\text{Volume of AGHE} = \left(\frac{1}{2} \times \text{base} \times \text{height} \right) \times \text{breadth}$$

$$= \left(\frac{1}{2} \times \text{HE} \times \text{GH} \right) \times 15$$

$$= \left(\frac{1}{2} \times 11.167 \times 0.129 \right) \times 15$$

$$\text{Free water vol.} = 10.804 \text{ m}^3$$

$$\text{Volume of oil in tank} = \text{T.O.V} - \text{free water}$$

$$= 2938.8 - 10.804$$

$$\text{G.O.V @ } 26^\circ\text{C} = 2927.996 \text{ m}^3$$

$$\text{VCF @ } 26^\circ\text{C} = 0.9905$$

$$\text{G.S.V} = 2900.18 \text{ m}^3$$

$$\text{Density in air/WRF (T56)} = 0.8189$$

$$\text{weight} = 2374.957 \text{ M.T}$$

JAN
2018
JULY
2023
JAN
2025

Find the final ullage using a VTI gauge, when 3200 M.T of Gas oil (density 0.8860 ts/m³ in vacuum) is blended with 2300 cubic meter of Diesel oil at 43°C (density 0.8693 ts/m³ in vacuum) in a box shaped tank 28.5m x 18.0m x 15.0m on-board a ship of LBP 196.4m, trimmed 1.2m by head and listed 3° to port. Ullage port for this tank is located 5.8m forward of the after bulkhead, 4.7m to starboard of the centerline and 112 cm above the top of the tank. Final temperature on completion of blending was found to be 20.0°C.

Note:- Syllabus does not include comingling. Comingling density does not need to be found out.

Therefore proceed as follows:-

$$\text{① Grade (gas oil) - density } 0.8860 = 3200 \text{ m.t}$$

$$W.C.F = \text{TS}_6$$

$$\text{Density in air} = 0.8849 \text{ t/m}^3 (0.8860 - 0.0011)$$

$$\text{Weight} = G.S.V @ 15^\circ\text{C} \times \text{density in air @ } 15^\circ\text{C}$$

$$3200 = G.S.V @ 15^\circ\text{C} \times 0.8849$$

$$G.S.V @ 15^\circ\text{C} = 3616.228 \text{ m}^3$$

Since final temp is 20°C ,

$$\text{So, VCF @ } 20^\circ\text{C} = 0.9962$$

$$G.S.V @ 15^\circ\text{C} = G.O.V @ 20^\circ\text{C} \times \text{VCF @ } 20^\circ\text{C}$$

$$3616.228 = G.O.V @ 20^\circ\text{C} \times 0.9962$$

$$G.O.V @ 20^\circ\text{C} = 3630.022 \text{ m}^3 \text{ ——— ①}$$

② Grade 2 (diesel oil) - density 0.8693

$$G.O.V @ 43^\circ\text{C} = 2300 \text{ m}^3$$

$$\text{V.C.F @ } 43^\circ\text{C} = 0.9785$$

$$\text{V.C.F @ } 20^\circ\text{C} = 0.9961$$

$$\frac{G.O.V @ 20^\circ\text{C}}{G.O.V @ 43^\circ\text{C}} = \frac{\text{VCF @ } 43^\circ\text{C}}{\text{VCF @ } 20^\circ\text{C}}$$

$$\frac{G.O.V @ 20^\circ\text{C}}{2300} = \frac{0.9785}{0.9961}$$

$$G.O.V @ 20^\circ\text{C} = 2259.361 \text{ m}^3 \text{ ——— ②}$$

$$\text{Eqn ① + ②}$$

$$= G.O.V @ 20^\circ\text{C of combined grade}$$

$$= 3630.022 + 2259.361$$

$$= 5889.383 \text{ m}^3$$

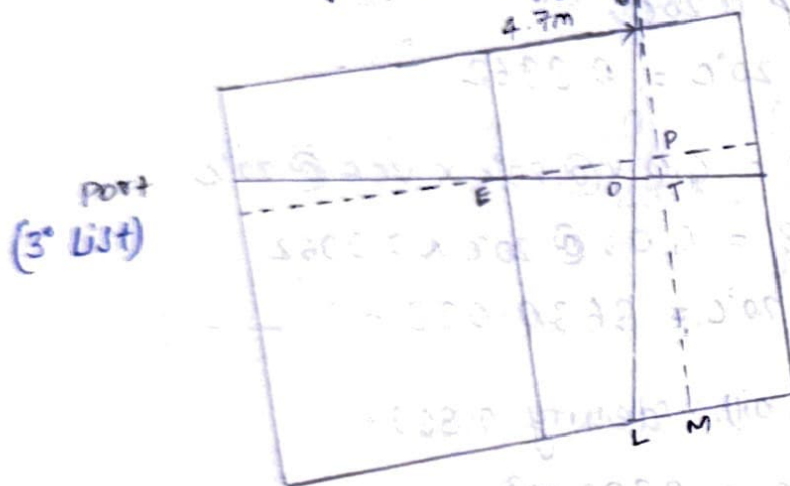
corrected sounding for coning grade = 7.7 m

$$= -G.O.V$$

$$L \times B$$

$$= \frac{5889.383}{28.5 \times 18}$$

$$PM = 11.480 \text{ m}$$



In ΔPTE ,

$$\tan \theta = \frac{PT}{PE}$$

$$\tan 3^\circ = \frac{PT}{4.7}$$

$$PT = 0.25 \text{ m}$$

$$UM = UP + PM$$

$$UP = UM - PM$$

$$UP = (15 + 1.12) - 11.480$$

$$UP = 16.12 - 11.480$$

$$UP = 4.64 \text{ m}$$

$$UT = UP + PT$$

$$= 4.64 + 0.25$$

$$= 4.89 \text{ m}$$

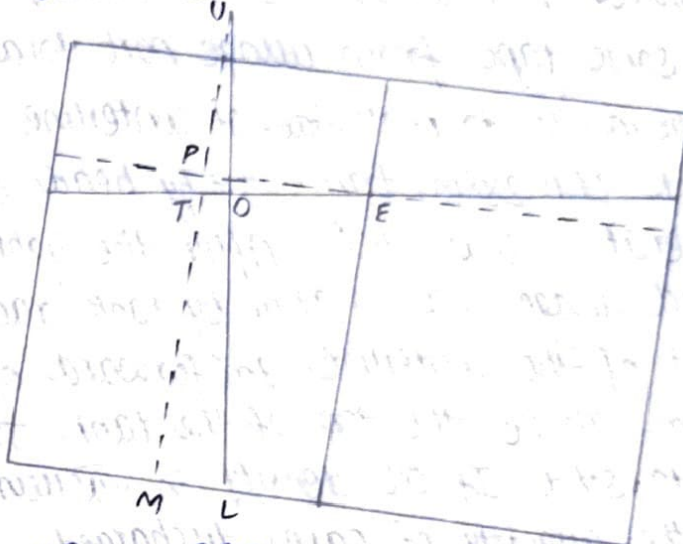
In ΔUOT ,

$$\cos \theta = \frac{UO}{UT}$$

$$\cos 3^\circ = \frac{UO}{4.89}$$

$$UO = 4.883m$$

Aft



Fwd
(1.2m by head)

$$UO = UP = 4.883$$

$$PE = \frac{L}{2} - d$$

$$= \frac{28.5}{2} - 5.8$$

$$= 8.45m$$

In ΔPTE ,

$$\tan \theta = \frac{PT}{PE}$$

$$\frac{TRIM}{LBP} = \frac{PT}{PE}$$

$$\frac{1.2}{196.4} = \frac{PT}{8.45}$$

$$PT = 0.052$$

$$\tan \theta = \frac{TRIM}{LBP}$$

$$\tan \theta = \frac{1.2}{196.4}$$

$$\theta = 0.35^\circ$$

$$UT = UP + PT$$

$$UT = 4.883 + 0.052$$

$$UT = 4.935m$$

In ΔUOT ,

$$\cos \theta = \frac{UO}{UT}$$

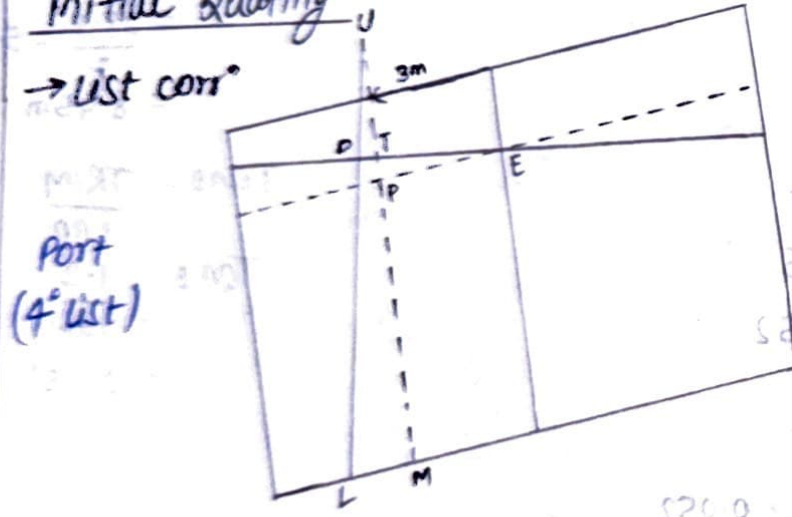
$$\cos 0.35^\circ = \frac{UO}{4.935}$$

$$UO = 4.935m$$

Ans

An oil tank measured $32 \times 20 \times 19\text{m}$. On arrival port 3.22m ullage was measured by sonic tape from ullage port located 4m forward of the after bulkhead, 3m to port side of centerline and 1.82m above the top of the tank. LBP 288m , trim 3.5m by head and list 4 degrees to port. Cargo temperature was 31.5°C . After the lighterage, cargo temperature was 27°C and ullage was 14.22m by tank radar which was located 4m to port of the centerline, 9m forward of the after bulkhead and 92cm above the top of the tank. Trim 2m by stern and list 3 degree to starboard. If oil density in vacuum at 15°C is 0.8311 t/m^3 . Find the quantity of cargo discharged.

→ List corr.



In ΔOOT ,

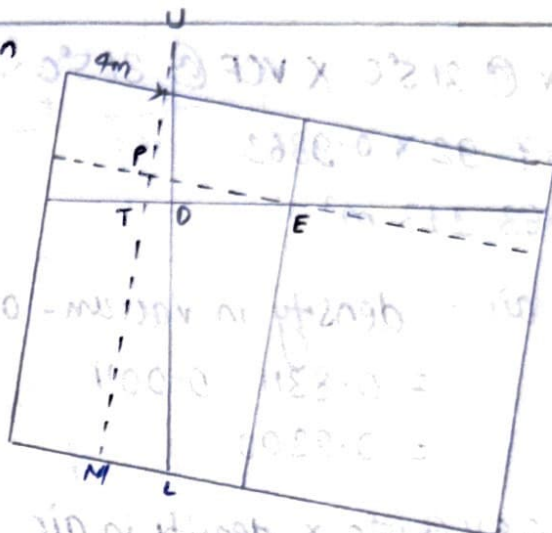
$$\cos \theta = \frac{OO'}{OT}$$
$$\cos 4^\circ = \frac{3.22}{UT}$$
$$UT = 3.228 \text{ m}$$

IN ΔPTE ,

$$\tan \theta = \frac{PT}{PE}$$
$$\tan 4' = \frac{PT}{3}$$
$$PT = 0.210$$

$$\begin{aligned} UP &= UT + PT \\ &= 3.228 + 0.210 \\ &= 3.438 \text{ m} \end{aligned}$$

→ Trim corrⁿ



$$UP = UO = 3.438m$$

Aft

Fwd
(3.5° by head)

In ΔUOT ,

$$\cos \theta = \frac{UO}{UT}$$

$$\cos 0.696^\circ = \frac{3.438}{UT}$$

$$UT = 3.438m$$

In ΔPTE ,

$$\tan \theta = \frac{PT}{PE}$$

$$\frac{TRIM}{LBP} = \frac{PT}{PE}$$

$$\frac{3.5}{288} = \frac{PT}{12}$$

$$PT = 0.146m$$

$$UT = UP + PT$$

$$UP = UT - PT$$

$$UP = 3.438 - 0.146$$

$$UP = 3.292m$$

$$UM = UP + PM$$

$$PM = UM - UP$$

$$PM = 20.82 - 3.292$$

$$PM = 17.528m$$

$$\begin{aligned} G.O.V @ 31.5^\circ C &= L \times B \times Sounding \\ &= 32 \times 20 \times 17.528 \\ &= 11217.92 m^3 \end{aligned}$$

$$VCF @ 31.5^\circ C = 0.9862$$

$$\tan \theta = \frac{TRIM}{LBP}$$

$$\tan \theta = \frac{3.5}{288}$$

$$\theta = 0.696^\circ$$

$$PE = \frac{l}{2} - d$$

$$= \frac{32}{2} - 4$$

$$= 16 - 4$$

$$= 12$$

$$\begin{aligned} UM &= 19 + 1.82 \\ &= 20.82m \end{aligned}$$

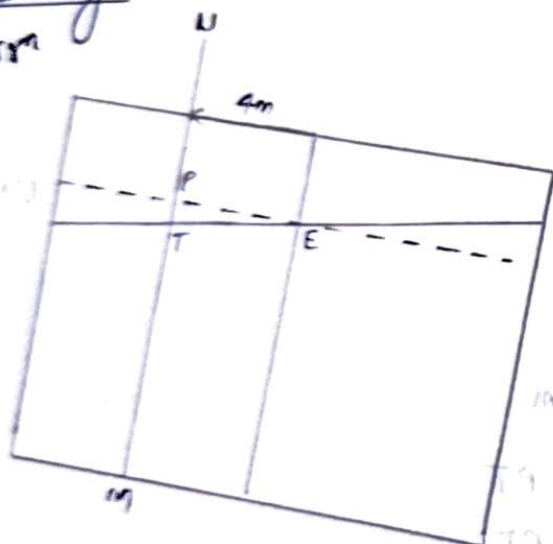
$$\begin{aligned}
 G.S.V @ 15^{\circ}C &= G.O.V @ 31.5^{\circ}C \times VCF @ 31.5^{\circ}C \\
 &= 11217.92 \times 0.9862 \\
 &= 11063.113 \text{ m}^3
 \end{aligned}$$

$$\begin{aligned}
 WCF/WRF/\text{density in air} &= \text{density in vacuum} - 0.0011 \\
 &= 0.8311 - 0.0011 \\
 &= 0.8300
 \end{aligned}$$

$$\begin{aligned}
 \text{Quantity of oil} &= G.S.V @ 15^{\circ}C \times \text{density in air} \\
 &= 11063.113 \times 0.8300 \\
 &= 9182.384 \text{ MT}
 \end{aligned}$$

Final Quantity

→ List corr



In ΔPTE,

$$\tan \theta = \frac{PT}{PE}$$

$$\tan 3^{\circ} = \frac{PT}{4}$$

$$PT = 0.210 \text{ m}$$

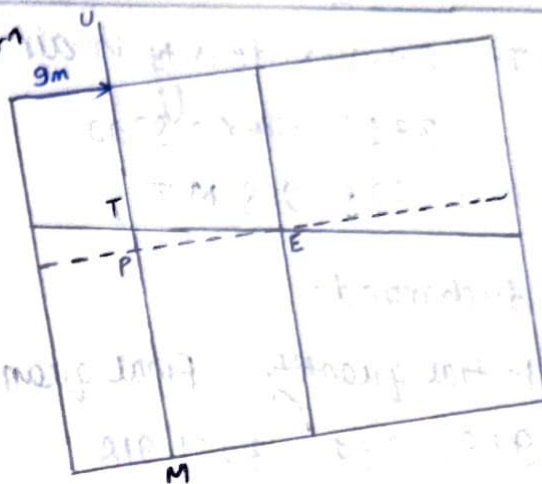
$$UT = UP + PT$$

$$UP = UT - PT$$

$$= 14.22 - 0.210$$

$$= 14.01 \text{ m}$$

→ Trim corr



$$UstUP = UT = 14.010m$$

Fwd

Aft
(2m by stern)

In ΔPTE ,

$$\tan \theta = \frac{PT}{PE}$$

$$\frac{TRIM}{LBP} = \frac{PT}{PE}$$

$$\frac{2}{288} = \frac{PT}{7}$$

$$PT = 0.049m$$

$$PE = \frac{l}{2} - d$$

$$PE = \frac{32}{2} - 9$$

$$PE = 16 - 9$$

$$PE = 7m$$

$$UM = 19 + 0.92$$

$$= 19.92m$$

Corrected
usage,

$$UP = UT + PT$$

$$= 14.010 + 0.049$$

$$= 14.059m$$

$$UM = UP + PM$$

Corrected sounding, $PM = UM - UP$

$$PM = 19.92 - 14.059$$

$$PM = 5.861m$$

$$G.O.V @ 27^{\circ}C = L \times B \times \text{sounding}$$

$$= 32 \times 20 \times 5.861$$

$$= 3751.04 m^3$$

$$VCF @ 27^{\circ}C = 0.9899$$

$$G.S.V @ 15^{\circ}C = G.O.V @ 27^{\circ}C \times VCF @ 27^{\circ}C$$

$$= 3751.04 \times 0.9899$$

$$= 3713.154 m^3$$

$$WCF/WRF/density in air = 0.8311 - 0.0011$$

$$= 0.8300$$

Quantity of oil in M.T = $G.S.V \times \text{density in air}$

$$= 3713.154 \times 0.8300$$

$$= 3081.918 \text{ M.T}$$

Quantity of cargo discharged =

Initial quantity - Final quantity

$$= 9182.384 - 3081.918$$

$$= 6100.466 \text{ M.T}$$

A box shaped cargo oil tank of dimension $30\text{m} \times 20\text{m} \times 18\text{m}$ is to be loaded with crude oil at a temperature of 25°C . Density of oil at 15°C in vacuum is 0.8240 . If 2% of the volume of the tank is to be left for expansion. Calculate

a) The final observed ullage by the measuring tape at the ullage port located 3m forward of aft bulkhead, 1m above the tank and 2m port of centerline

b) Quantity of oil loaded on-board (LOP = 220m, Trim 3m by Stern and list 1° to Stbd)

$$\text{Volume of tank} = 30 \times 20 \times 18$$

$$= 10,800 \text{ m}^3$$

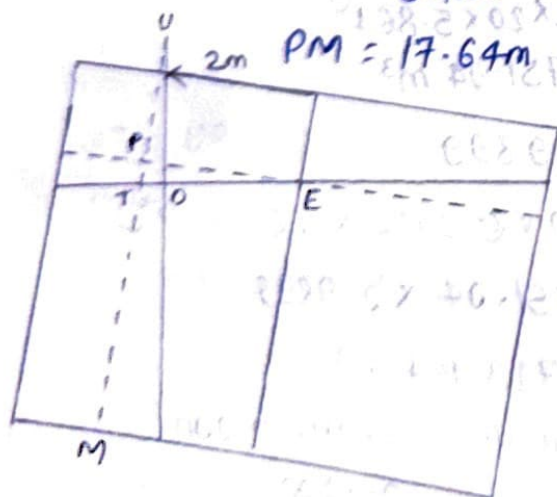
$$2\% \text{ to be left for expansion} = \frac{216}{100}$$

$$\text{Volume left for loading} = 10584 \text{ m}^3$$

$$\text{Sounding in tank, PM} = \frac{10584}{30 \times 20}$$

$$PM = 17.64\text{m}$$

Port



Stbd
(1° list)

17 + 15 = 32

79-70-70

MILES 1

MILES 1

520 21

0.8000

NO. 1534

$\in [10, 10 + \epsilon]$

A

$$\varepsilon_m 48201 = 0.25 \text{ @ } v.o.p.$$

Not a student of this school

Perpet = 3021 911.2.2

1201904



1. WOUT
 2. SCSS
 3. WAD
 4. FLOS
 5. VOM
 6. ISGS

$$PE = \frac{1}{2} - d$$

$$\frac{MRT}{PE} = 0.207$$

$$PE = \frac{30}{2} - 3$$

PE = 15-3
PE = 12m

$$0.52 - 0.52 = 0$$

102

$$UP = UT + PT$$

$$UT = UP - PT$$

$$= 1.395 - 0.164 = 1.231$$

$$= 1.231 m$$

In ΔUOT ,

$$\cos \theta = \frac{UO}{UT}$$

$$\cos 0.8^\circ = \frac{UO}{1.231}$$

Observed ullage $UO = 1.231$

b) Qty of oil $\Rightarrow$

$$G.O.V @ 25^\circ C = 10584 m^3$$

$$VCF @ 25^\circ C = 0.9915 \quad (0.8240)$$

$$G.S.V @ 15^\circ C = 10494.036$$

$$WCF/WRF = 0.8229 \quad (0.8240 - 0.0011)$$

$$\text{Weight} = 8635.54 t$$

A crude oil tanker of LBP 228m has a box shaped tank of dimensions 32x20x20m & trimmed 1m by stern. Initial ullage of 0.60m is measured by Radar beam level guage fitted 3m forward of aft bulkhead on centerline of tank. Given the density of oil at 15°C = 0.810 t/m³ and observed temp is 24°C. On completion of unloading vessel trimmed 3.8m by stern & ullage of tank was 19.88m. calculate the quantity of oil discharged.

$$\tan \theta = \frac{\text{TRIM}}{\text{LBP}}$$

$$\tan \theta = \frac{1}{228}$$

$$\theta = 0.25^\circ$$

$$PE = \frac{l}{2} - d$$

$$PE = \frac{32}{2} - 3$$

$$= 16 - 3$$

$$= 13m$$

JULY
2016,
JAN
2017,
NOV
2021

Som:-

$$UM = UT + TM$$

$$TM = UM - UT$$

$$= 20 - 19.88$$

$$= 0.12m$$

In $\triangle TME$

$$\tan \theta = \frac{TM}{ME}$$

$$\frac{TRIM}{LBP} = \frac{TM}{ME}$$

$$\frac{3.8}{228} = \frac{0.12}{ME}$$

$$ME = 7.2m$$

$$HM = 3.0m$$

$$HE = HM + ME$$

$$= 3.0 + 7.2$$

$$= 10.2m$$

Length of the tank is 32m

Hence, wedge is confirmed

In $\triangle GHE$

$$\tan \theta = \frac{GH}{HE}$$

$$\frac{TRIM}{LBP} = \frac{GH}{HE}$$

$$\frac{3.8}{228} = \frac{GH}{10.2}$$

$$GH = 0.17m$$

$$\text{Final volume of oil} = \left(\frac{1}{2} \times \text{base} \times \text{height} \right) \times \text{breadth}$$

$$= \left(\frac{1}{2} \times 10.2 \times 0.17 \right) \times 20$$

$$= 17.34m^3$$

Volume of oil discharged:

$$G.O.V @ 24^{\circ}C : 11605.8 - 17.34 \\ = 11588.46 m^3$$

$$VCF @ 24^{\circ}C = 0.9921$$

$$G.S.V @ 15^{\circ}C = 11588.46 \times 0.9921 \\ = 11496.91 m^3$$

$$WCF/WRF/density \text{ in air} = \text{density in vac.} - 0.0011 \\ = 0.810 - 0.0011 \\ = 0.8089$$

$$\text{Quantity of oil discharged} = 11496.91 \times 0.8089 \\ = \boxed{9299.85 T} \quad \text{Ans}$$

A box-shaped tank of a vessel had 3000 mt of cargo on arrival. To this, 2000 m³ of the same cargo of density 0.850 was added at temperature 30°C. Find the final observed ullage using a UTI tape from a point 4.0m fwd of the aft bulkhead, 1.0m above the deck and 4.0m to port of CL of tank when trim was 2.0m stern and list nil. Tank dimension 22x20x15 and LBP of vessel 220m. Final temperature 30°C. Also, find the total quantity of cargo. All weights in air.

$$Qty \text{ of oil} = G.S.V @ 15^{\circ}C \times \text{density in air}$$

$$3000 = G.S.V @ 15^{\circ}C \times 0.8489$$

$$(0.850 - 0.0011)$$

$$G.S.V @ 15^{\circ}C = 3533.985 m^3$$

$$G.S.V @ 15^{\circ}C = G.O.V @ 30^{\circ}C \times VCF @ 30^{\circ}C$$

$$3533.985 = G.O.V @ 30^{\circ}C \times 0.9880$$

$$G.O.V @ 30^{\circ}C = 3576.908 m^3$$

$$\text{Volume added, } G.O.V @ 30^{\circ}C = 2000 m^3$$

$$\text{Total vol., } G.O.V @ 30^{\circ}C = 5576.908 m^3$$

JULY
2024
Am,

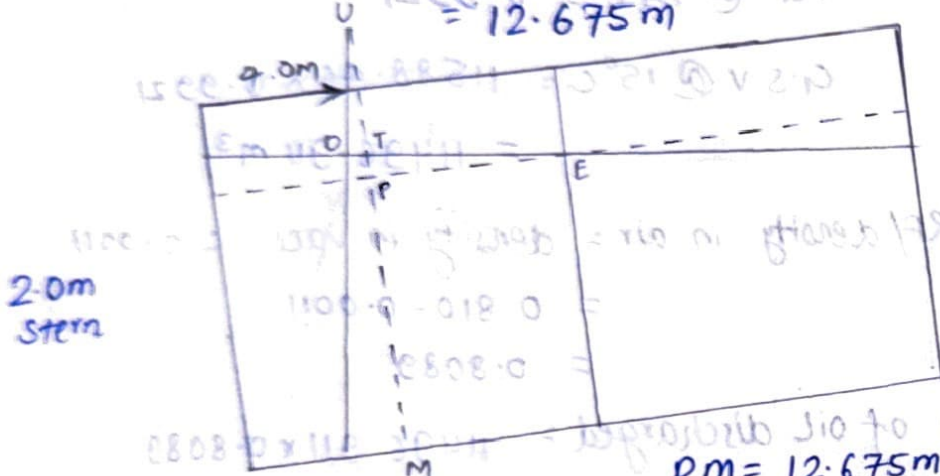
Soln.

Actual sounding = $\frac{\text{Vol. gradient}}{\text{LKB}}$ for 2m to 10m

$$PE = 11.8 \times \frac{1500}{1000} = 17.7 \text{ m}$$

$$= \frac{5576.908}{22 \times 20}$$

$$= 12.675 \text{ m}$$



In ΔPTE ,

$$\tan \theta = \frac{PT}{PE}$$

$$\frac{\text{TRIM}}{\text{LBP}} = \frac{PT}{PE}$$

$$\frac{2}{22} = \frac{PT}{7}$$

$$PT = 0.064 \text{ m}$$

$$UP = UT + PT$$

$$UT = UP - PT$$

$$= 3.325 - 0.064$$

$$= 3.261 \text{ m}$$

$$PM = 12.675 \text{ m}$$

$$UP = UM - PM$$

$$= (15.7) - 12.675 = 3.325 \text{ m}$$

$$\tan \theta = \frac{\text{TRIM}}{\text{LBP}}$$

$$\tan \theta = \frac{2}{22}$$

$$\theta = 0.52^\circ$$

In ΔUOT ,

$$\cos \theta = \frac{UO}{UT}$$

$$\cos 0.52^\circ = \frac{UO}{3.261}$$

$$\cos 0.52^\circ = \frac{UO}{3.261}$$

$$UO = 3.261 \text{ m}$$

i.e. final observed surge

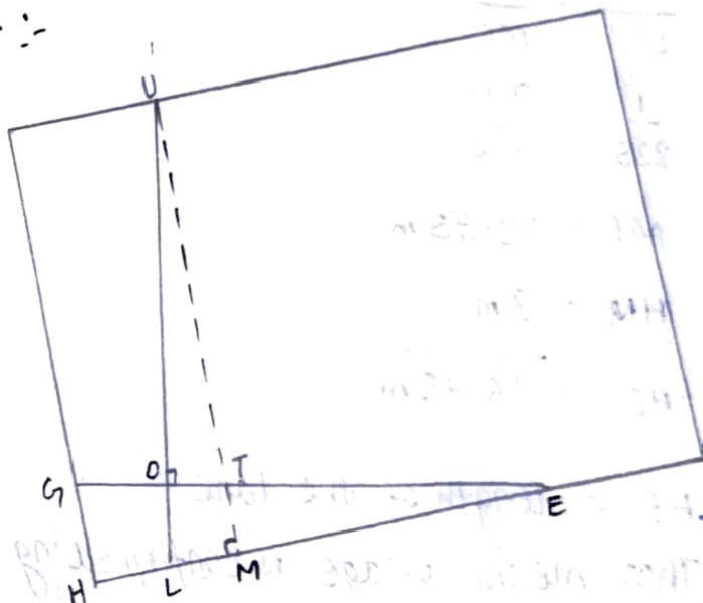
CHECK WEDGE, TRIM

DEC
2013
JULY
2018
JAN
2023
JAN
2025 AM

A box-shaped cargo tank 40m x 22m x 18m was observed to have a sounding of 15cm by sounding rod. ullage reference point was located at the tank top, 3m forward of aft bulkhead. vessel was trimmed 1m by stern and LBP of vessel was 255m. Upon completion of loading in the tank, vessel was even keel and ullage of tank by sonic guage was 1.10m. Calculate the quantity of oil loaded in the tank, if the observed temperature was 30°C and API gravity was 30.5 in both cases.

Soln:

Initial cond. :-



In ΔULM ,

$$\cos \theta = \frac{UM}{UL} \left(\frac{b}{h} \right)$$

$$\cos 0.225^\circ = \frac{18}{UL}$$

$$UL = 18.000m$$

$$UL = UO + OL$$

$$18 = UO + 0.15$$

$$UO = 18 - 0.15$$

$$UO = 17.85m$$

In ΔUOT ,

$$\cos \theta = \frac{UO}{UT}$$

$$\cos 0.225^\circ = \frac{17.85}{UT}$$

$$UT = 17.850m$$

$$\tan \theta = \frac{\text{TRIM}}{\text{LBP}}$$

$$\tan \theta = \frac{1}{255}$$

$$\theta = 0.225^\circ$$

$$UM = UT + TM$$

$$18 = 17.850 + TM$$

$$TM = 0.15m$$

In ΔTME ,

$$\tan \theta = \frac{TM}{ME}$$

$$\frac{TRIM}{LBP} = \frac{TM}{ME}$$

$$\frac{1}{255} = \frac{0.15}{ME}$$

$$ME = 38.25m$$

$$HM = 3m$$

$$HE = 41.25m$$

$HE >$ length of the tank

That means, wedge is not forming

In ΔPTE , $\tan \theta = \frac{PT}{PE}$

$$\frac{TRIM}{LBP} = \frac{PT}{PE}$$

$$\frac{1}{255} = \frac{PT}{17}$$

$$PT = 0.067m$$

$$UP = UT + PT$$

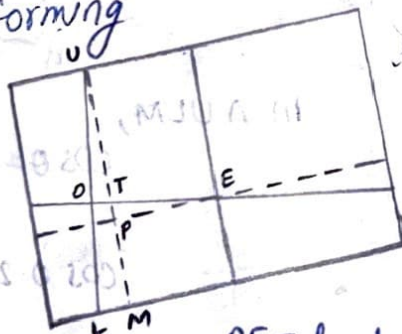
$$UP = 17.850 + 0.067$$

$$UP = 17.917m$$

$$UM = UP + PM$$

$$18 = 17.917 + PM$$

$$PM = 0.083m$$



$$PE = \frac{l}{2} - d$$

$$= \frac{40}{2} - 3$$

$$= 20 - 3$$

$$= 17$$

Volume of oil in tank = $L \times b \times \text{sounding}$

$$= 40 \times 22 \times 0.083$$

$$= 73.04 m^3$$

$$\text{i.e. } 61.0 \text{ v @ } 30^\circ C = 73.04 m^3$$

Final cond:

$$\text{Ullage} = 1.10 \text{ m}$$

$$\text{Sounding} = 18 - 1.10 = 16.90 \text{ m}$$

$$\text{Volume of cargo in tank} = L \times B \times \text{sounding}$$

$$= 40 \times 22 \times 16.90$$

$$G.O.V = 14872 \text{ m}^3$$

$$\text{Volume of oil loaded in tank} = \text{Final vol} - \text{Initial vol}$$

$$= 14872 - 73.04$$

$$= 14798.96 \text{ m}^3$$

↓
i.e. G.O.V @ 30°C

$$\text{Density at } 15^\circ\text{C (API: 30.5)} = 0.8730$$

$$V.C.F \text{ at } 30^\circ\text{C (density: 0.8730)} = 0.9882$$

$$G.S.V = G.O.V @ 30^\circ\text{C} \times VCF @ 30^\circ\text{C}$$

$$= 14798.96 \times 0.9882$$

$$= 14624.332 \text{ m}^3$$

$$W.C.F = \text{density in vac.} - 0.0011$$

$$= 0.8730 - 0.0011$$

$$= 0.8719$$

$$\text{Weight of oil} = G.S.V \times W.C.F$$

$$= 14624.332 \times 0.8719$$

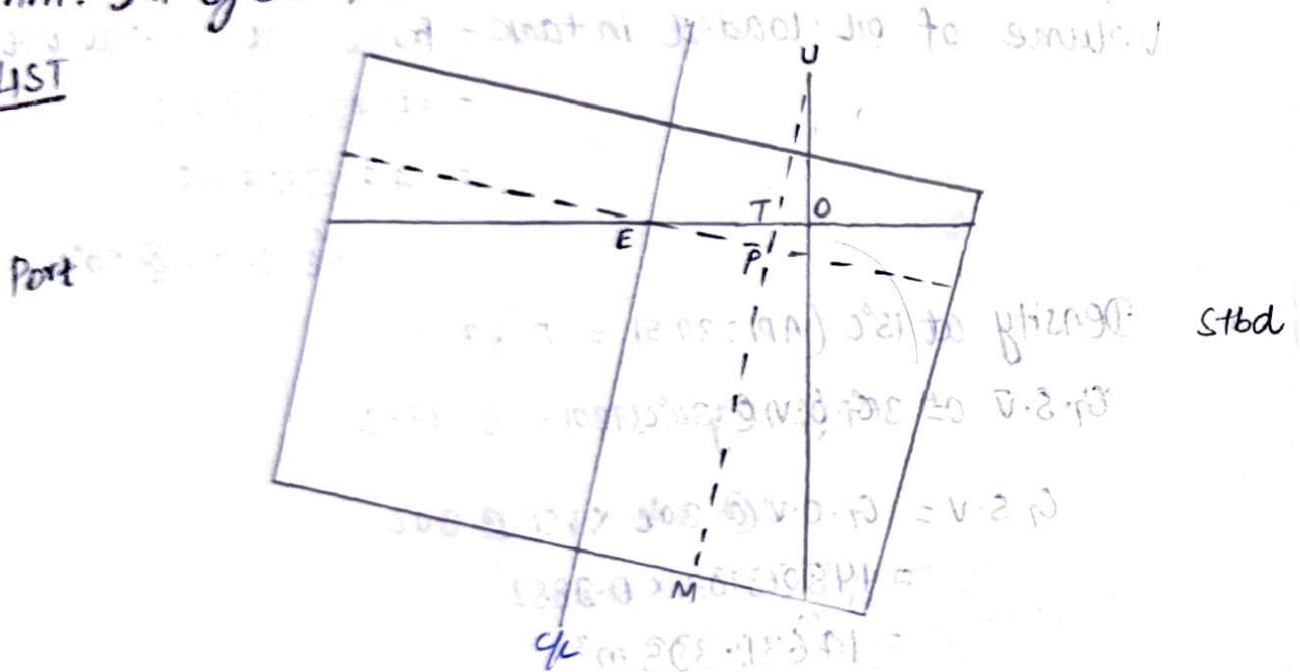
$$= 12750.955 \text{ t}$$

TRIM + LIST

OCT
2024 AM

On an oil tanker, a box shaped cargo tank measuring $26 \times 15 \times 17 \text{ m}$ is loaded with Diesel oil whose density at 15°C is 0.8424 . The final ullage by UTI tape is observed to be 1.86 m and temperature of cargo is 34.7°C . Find the quantity of cargo loaded if ullage port is 800 mm is above the tp of the tank, 5 m forward of aft bulkhead of tank and 4 m starboard of tank cl, LBP = 225 m , Trim: 5 m by stern, and 2.5° starboard

LIST



In ΔOOT ,

$$\cos \theta = \frac{U_0}{U_T}$$

$$\cos 2.5^\circ = \frac{1.86}{UT}$$

$$UT = 1.862 \text{ m}$$

IN ΔPTE ,

$$\tan \theta = \frac{PT}{PE}$$

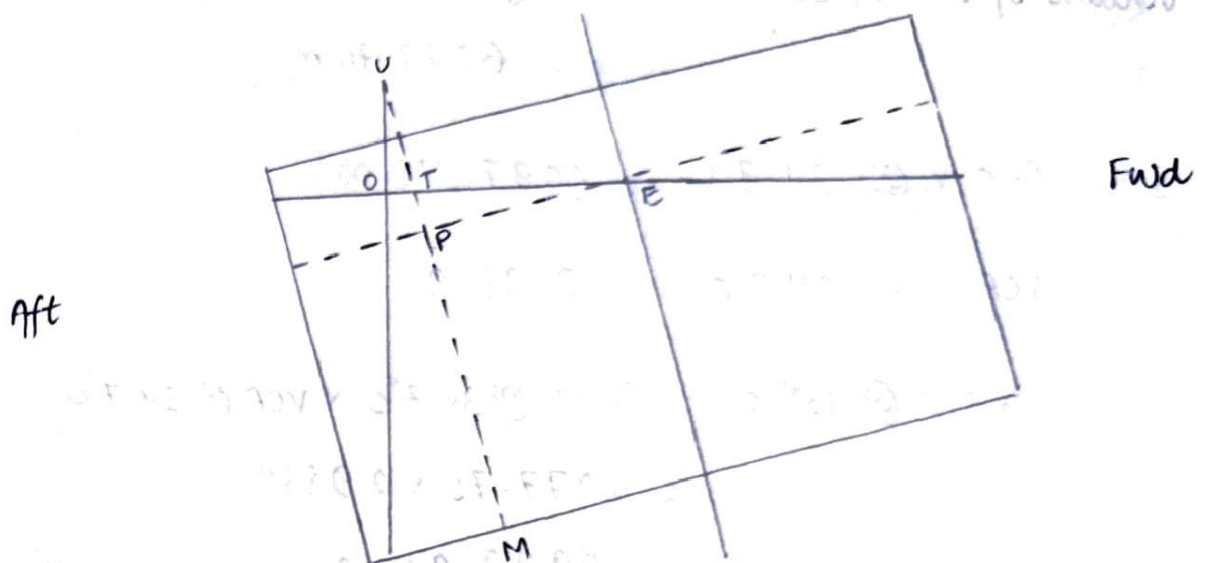
$$PE = 4m$$

$$\tan 2.5^\circ = \frac{PT}{4}$$

$$PT = 0.175 \text{ m}$$

$$\begin{aligned} UP &= UT + PT \\ &= 1.862 + 0.175 \\ &= 2.037m \end{aligned}$$

$$List\ UP = Trim\ UO = 2.037m$$



In ΔUOT ,

$$\cos \theta = \frac{UO}{UT}$$

$$\cos 1.27^\circ = \frac{2.037}{UT}$$

$$UT = 2.038m$$

$$\tan \theta = \frac{TRIM}{LOP}$$

$$\tan \theta = \frac{5}{225}$$

$$\theta = 1.27^\circ$$

In ΔPTE ,

$$\tan \theta = \frac{PT}{PE}$$

$$\frac{TRIM}{LOP} = \frac{PT}{PE}$$

$$\frac{5}{225} = \frac{PT}{8}$$

$$PT = 0.178$$

$$PE = \frac{d}{2} - d$$

$$= \frac{26}{2} - 5$$

$$= 13 - 5$$

$$= 8$$

$$UP = UT + PT$$

$$UP = 2.038 + 0.178$$

$$UP = 2.216m$$

$$UM = UP + PM$$

$$17 + 0.8 = 2.216 + PM$$

$$17.8 = 2.216 + PM$$

$$PM = 15.584$$

$$\text{volume of oil in cargo tank} = 26 \times 15 \times 15.584 \\ = 6077.76 \text{ m}^3$$

$$G.O.V @ 34.7^\circ\text{C} = 6077.76 \text{ m}^3$$

$$VCF @ 34.7^\circ\text{C} = 0.9839$$

$$G.S.V @ 15^\circ\text{C} = G.O.V @ 34.7^\circ\text{C} \times VCF @ 34.7^\circ\text{C} \\ = 6077.76 \times 0.9839 \\ = 5979.91 \text{ m}^3$$

$$WRF/WCF/\text{density in air} = \text{density in vacuum} - 0.0011 \\ = 0.8424 - 0.0011 \\ = 0.8413$$

$$\text{Quantity of oil loaded} = G.S.V @ 15^\circ\text{C} \times WCF/WRF \\ = 5979.91 \times 0.8413$$

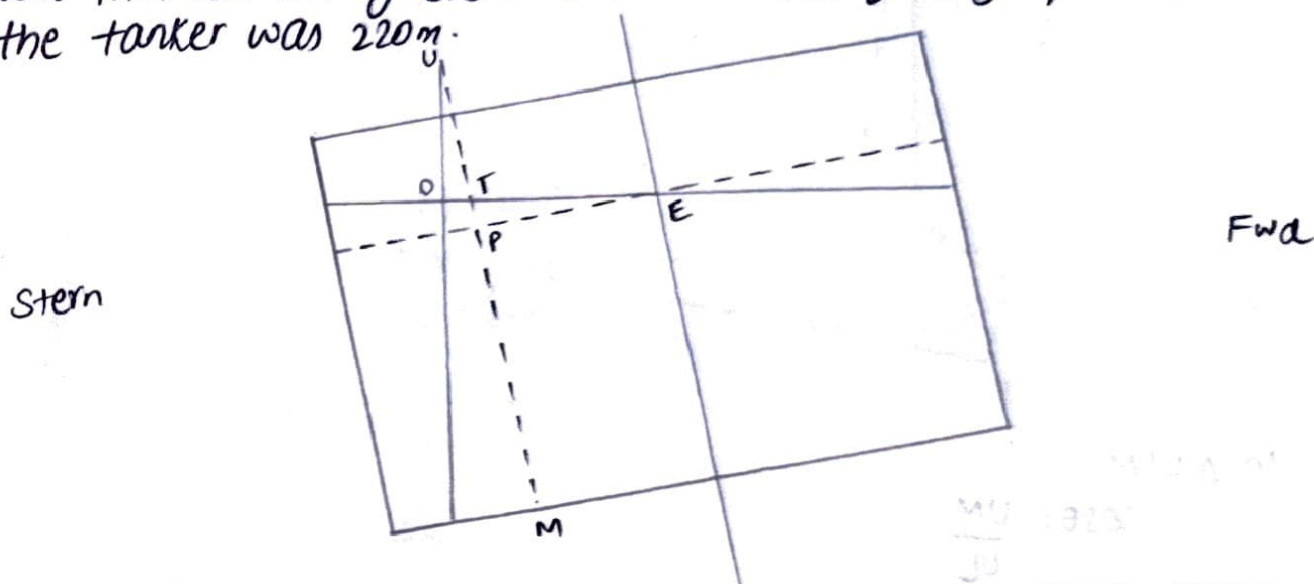
$$= 5030.9 \text{ T}$$

Ans

JULY
2024
PM

A box shaped tank L 28m, B 20m, D 18m, of an oil tanker containing crude oil of density at $15^{\circ}\text{C} = 0.8350 \text{ t/m}^3$ had an ullage of 1.40 as measured by UTI detector after loading and observed temperature was 32°C . A water dip 12cm was found. The ullage port was located 1.2m above the tank top and 2.0m forward of aft bulkhead. Ullage was trimmed 2m by stern. Determine the quantity of oil in tank. LBP of the tanker was 220m.

Ans:-



In ΔUOT ,

$$\cos \theta = \frac{UO}{UT}$$

$$\cos 0.52^{\circ} = \frac{1.4}{UT}$$

$$UT = 1.400 \text{ m}$$

In ΔPTE ,

$$\tan \theta = \frac{PT}{PE}$$

$$\frac{\text{TRIM}}{\text{LBP}} = \frac{PT}{PE}$$

$$\frac{2}{220} = \frac{PT}{12}$$

$$PT = 0.109$$

$$UP = UT + PT$$

$$UP = 1.400 + 0.109$$

$$UP = 1.509 \text{ m}$$

$$UM = UP + PM$$

$$18 + 1.2 = 1.509 + PM$$

$$PM = 17.691 \text{ m}$$

$$\tan \theta = \frac{\text{TRIM}}{\text{LBP}}$$

$$\tan \theta = \frac{2}{220}$$

$$\theta = 0.52^{\circ}$$

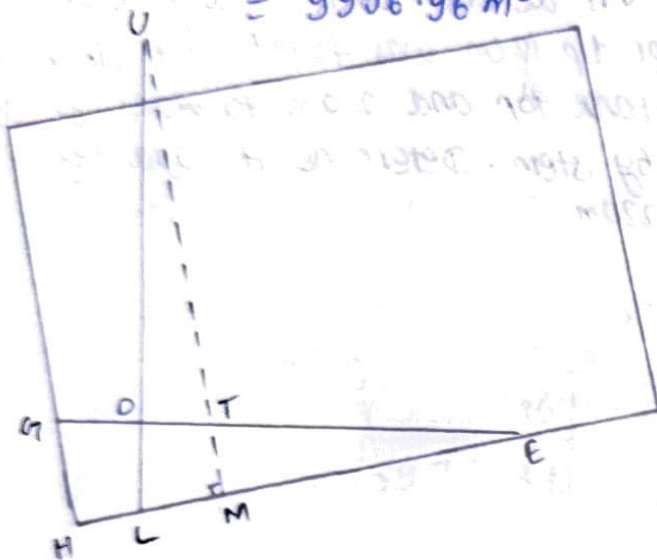
$$PE = \frac{L}{2} - d$$

$$= \frac{28}{2} - 2$$

$$= 14 - 2$$

$$= 12$$

Volume of liquid in tank = $L \times B \times \text{sounding}$
 $= 28 \times 20 \times 17.691$
 $= 9906.96 \text{ m}^3$



in a ULM,

$$\cos \theta = \frac{v_M}{v_L}$$

$$\cos 0.52^\circ = \frac{19.2}{UL}$$

$$UL = 19.200 \text{ m}$$

$$U_L = U_0 + OL$$

$$19.2 = 0.0 + 0.12$$

$$U_0 = 19.080 \text{ m}$$

In ΔUOT ,

$$\cos \theta = \frac{U_0}{UT}$$

$$\cos 0.52^\circ = \frac{19.080}{U_T}$$

$$UT = 19.081 \text{ m}$$

$$UM = UT + TM$$

$$19.2 = 19.081 + TM$$

$$T_M = 19.2 - 19.081$$

$$T_M = 0.119 \text{ m}$$

IN ΔTME ,

$$\tan \theta = \frac{TM}{ME}$$

$$\frac{TRIM}{LBP} = \frac{TM}{ME}$$

$$\frac{2}{220} = \frac{0.119}{ME}$$

$$ME = 13.09 \text{ m}$$

$$HM = 2 \text{ m}$$

$$HE = HM + ME$$

$$HE = 2 + 13.09$$

$$HE = 15.09 \text{ m} \quad \text{i.e. less than length of the vessel}$$

wedge is confirmed.

IN ΔGHE ,

$$\tan \theta = \frac{GH}{HE}$$

$$\frac{TRIM}{LBP} = \frac{GH}{HE}$$

$$\frac{2}{220} = \frac{GH}{15.09}$$

$$GH = 0.137 \text{ m}$$

$$\text{Volume of water in tank } (\Delta GHE) = \left(\frac{1}{2} \times HE \times GH \right) \times \text{breadth}$$

$$= \frac{1}{2} \times 15.09 \times 0.137 \times 20$$

$$= 20.673 \text{ m}^3$$

$$\text{Volume of oil in tank} = \text{Total liquid} - \text{vol. of water}$$

$$= 9906.96 - 20.673$$

$$= 9886.287 \text{ m}^3$$

$$G.O.V @ 32^\circ\text{C} = 9886.287 \text{ m}^3$$

$$VCF @ 32^\circ\text{C} = 0.9859$$

$$G.S.V @ 15^\circ\text{C} = 9746.89 \text{ m}^3$$

$$WCF/WRF = 0.8350 - 0.0011 = 0.8339$$

$$\text{Quantity of oil} = 9746.89 \times 0.8339$$

$$= \boxed{8127.932 \text{ T}} // \text{Ans}$$