

OCT 2024 MV Pilot is loaded up ready for departure,  $K_G$  is 6.55m, FSM 1350 tm, with a displacement of 9000 t. From the cross curves of stability, the KN values are:

|      |   |      |      |      |      |      |      |
|------|---|------|------|------|------|------|------|
| HEEL | 0 | 15   | 30   | 45   | 60   | 75   | 90   |
| KN   | 0 | 1.98 | 4.10 | 5.92 | 6.82 | 6.98 | 6.58 |

Construct the statical stability curve for this condition and determine the following range of stability. Change of above range when transverse upsetting moment of 2250 tm is caused. Moment of stability stability at 5° heel.

The maximum GZ and angle at which it occurs, Dynamical stability at 45°

Sol<sup>n</sup>:-

$$K_G : 6.55 \text{ m}$$

$$FSC : 0.15 \text{ m } (1350/9000)$$

$$\text{corrected } K_G : 6.70 \text{ m}$$

|                                 |   |       |       |       |       |       |       |
|---------------------------------|---|-------|-------|-------|-------|-------|-------|
| HEEL                            | 0 | 15    | 30    | 45    | 60    | 75    | 90    |
| KN                              | 0 | 1.98  | 4.10  | 5.92  | 6.82  | 6.98  | 6.58  |
| $K_G \sin \theta$               | 0 | 1.734 | 3.350 | 4.738 | 5.802 | 6.472 | 6.7   |
| GZ<br>(KN - $K_G \sin \theta$ ) | 0 | 0.246 | 0.750 | 1.182 | 1.018 | 0.508 | -0.12 |

PLOT THE GZ CURVE

$$\text{Moment of statical stability} = W \times GZ$$

$$2250 = 9000 \times GZ$$

$$GZ = 0.25 \text{ m (plot on GZ curve)}$$

$$\text{Range of +ve stability} = 0^\circ \text{ to } 87^\circ$$

$$\text{Range of +ve stability after upsetting moment is caused} = 15^\circ \text{ to } 82^\circ \quad \left. \vphantom{\text{Range of +ve stability after upsetting moment is caused}} \right\} \text{Ans}$$

$$\text{Max}^m \text{ GZ} : 1.2 \text{ m}$$

$$\text{Dynamical stability at } 45^\circ = \text{Area under curve upto } 45^\circ \times W$$

$$\text{Heel GZ SM POA} = 0.409 \times 9000$$

$$0 \quad 0 \quad 1 \quad 0 = 3681 \text{ mrt} \quad \text{Ans}$$

$$15 \quad 0.246 \quad 3 \quad 0.738$$

$$30 \quad 0.750 \quad 3 \quad 2.25$$

$$45 \quad 1.182 \quad 1 \quad 1.182$$

$$SOPA = 4.17$$

$$\text{Area under curve upto } 45^\circ$$

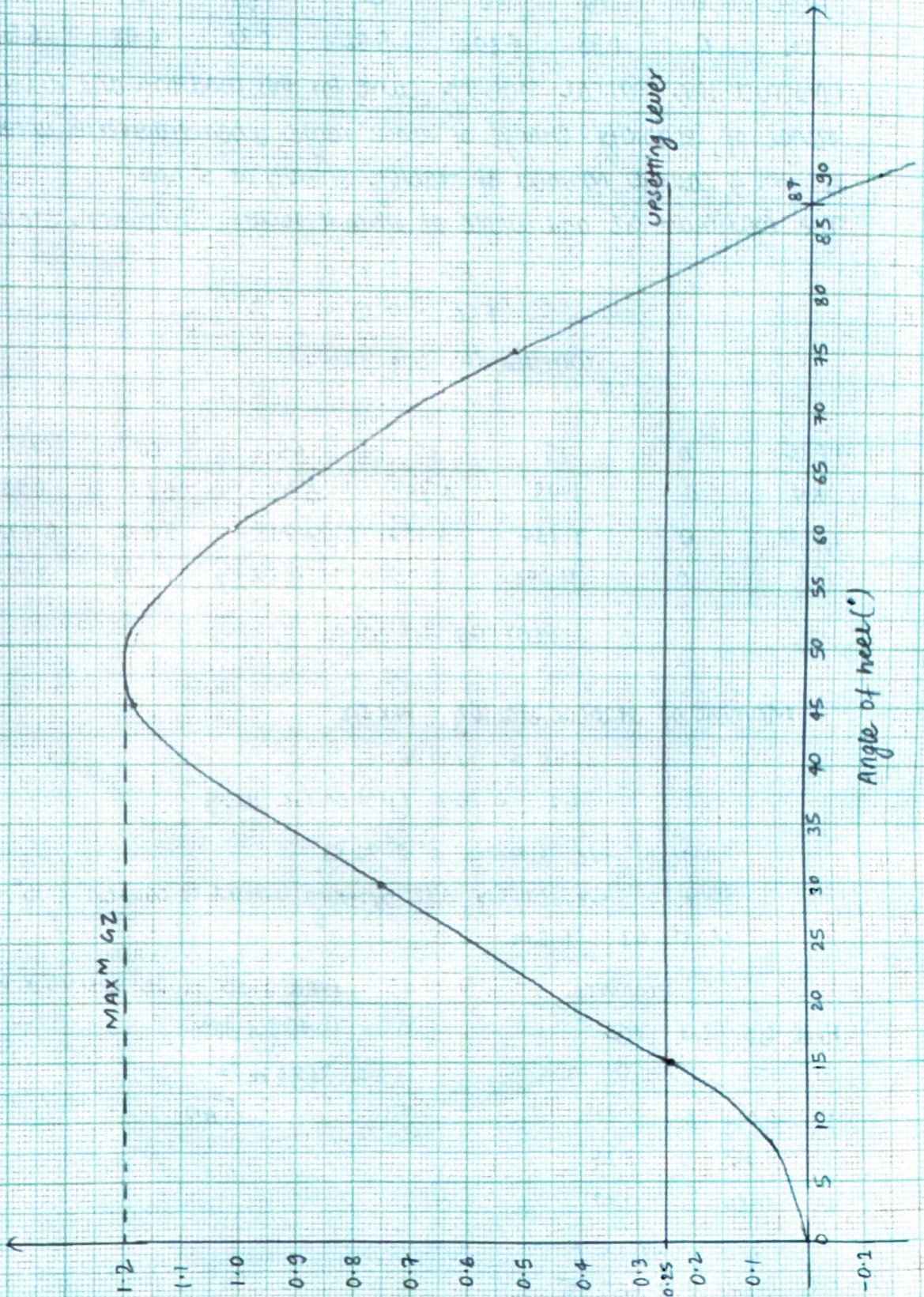
$$= \frac{SOPA \times 3h}{8} = \frac{4.17 \times 3 \times 15}{8 \times 57.3} = 0.409 \text{ meter radian}$$

to convert into meter radian

SCALE;

ANGLE OF HEEL ( $^{\circ}$ ): 1CM =  $5^{\circ}$ 

GZ (in metres) : 1CM = 0.1 metres



|            |                                          |   |      |     |      |     |
|------------|------------------------------------------|---|------|-----|------|-----|
| JULY 2024, | A ship has displacement 15000t $K_G$ 7.0 |   |      |     |      |     |
| JAN 2023,  | Heel                                     | 0 | 15   | 30  | 45   | 60  |
| OCT 2018   | GZ                                       | 0 | 0.38 | 1.0 | 1.41 | 1.2 |

The vessel has loaded to this displacement, but  $K_G$  is found to be 6.8m. Draw the amended GZ curve, confirm whether the vessel complies with the intact stability criteria. calculate the dynamic stability at 60° heel.

|       |                                                            |   |        |        |       |        |
|-------|------------------------------------------------------------|---|--------|--------|-------|--------|
| SOP:- | Heel                                                       | 0 | 15     | 30     | 45    | 60     |
|       | GZ                                                         | 0 | 0.38   | 1.0    | 1.41  | 1.2    |
|       | corr to GZ<br>$G_{G2}(\downarrow) SO (H_{G2}) \sin \theta$ | 0 | +0.052 | +0.100 | 0.141 | +0.173 |
|       | where $G_{G2} = 7.0 - 6.8 = 0.2$                           |   |        |        |       |        |
|       | corrected GZ                                               | 0 | 0.432  | 1.100  | 1.551 | 1.373  |

Area upto 30° heel

| Heel | GZ    | SM | POA   |
|------|-------|----|-------|
| 0    | 0     | 1  | 0     |
| 15   | 0.432 | 4  | 1.728 |
| 30   | 1.100 | 1  | 1.1   |

SOPA: 2.828

$$\text{Area}_{\text{upto } 30^\circ} = \frac{\text{SOP} \times h}{3} = \frac{2.828 \times 15}{3 \times 57.3}$$

$$= 0.247 \text{ MR}$$

Area upto 40° heel

| Heel | GZ   | SM | POA  |
|------|------|----|------|
| 0    | 0    | 1  | 0    |
| 10   | 0.21 | 4  | 0.84 |
| 20   | 0.66 | 2  | 1.32 |
| 30   | 1.10 | 4  | 4.4  |
| 40   | 1.5  | 1  | 1.5  |

SOPA: 8.06

$$\text{Area}_{\text{upto } 40^\circ} = \frac{8.06 \times 10}{3 \times 57.3} = 0.469 \text{ MR}$$

$$\text{Area } 30^\circ \text{ to } 40^\circ = 0.430 - 0.247 = 0.183$$

(A) Area under curve upto 30° to be not less than 0.055 metre radian

$$\text{Area upto } 30^\circ = 0.247 \text{ metre radian} \therefore \text{COMPLIED}$$

(B) Area under curve upto 40° to be not less than 0.09 metre radian

$$\text{Area upto } 40^\circ = 0.469 \text{ metre radian} \therefore \text{COMPLIED}$$

(C) Area between 30° and 40° to be not less than 0.03 metre radian

$$\text{Area b/w } 30^\circ \text{ to } 40^\circ = 0.183 \text{ metre radian} \therefore \text{COMPLIED}$$

(E) Max<sup>m</sup> GZ to occur at angle not less than 30° and to be atleast 0.20m

$$\text{Max}^m \text{ GZ occurred at } 48^\circ \text{ i.e. } \text{not less than } 30^\circ \therefore \text{COMPLIED}$$

$$\text{Max}^m \text{ GZ: } 1.55 \text{m, should be atleast } 0.20 \therefore \text{COMPLIED}$$

Ⓕ Initial GM to be not less than 0.15 metres

Initial GM: 0.95 : COMPLIED

Now to calculate dynamic stability at 60° heel

Area upto 60° heel

| Heel | GZ    | SM | POA   |
|------|-------|----|-------|
| 0    | 0     | 1  | 0     |
| 15   | 0.432 | 4  | 1.728 |
| 30   | 1.100 | 2  | 2.200 |
| 45   | 1.551 | 4  | 6.204 |
| 60   | 1.373 | 1  | 1.373 |

$$SOPA = 10.505$$

$$\text{Area upto } 60^\circ \text{ heel} = \frac{SOPA \times h}{3}$$

$$= \frac{11.505 \times 15}{3 \times 57.3}$$

$$= 57.525 \text{ m}^2$$

$$= 1.004 \text{ m/r}$$

Dynamical stability at 60° = Area under curve upto 60° × W

$$= 1.004 \times 15000$$

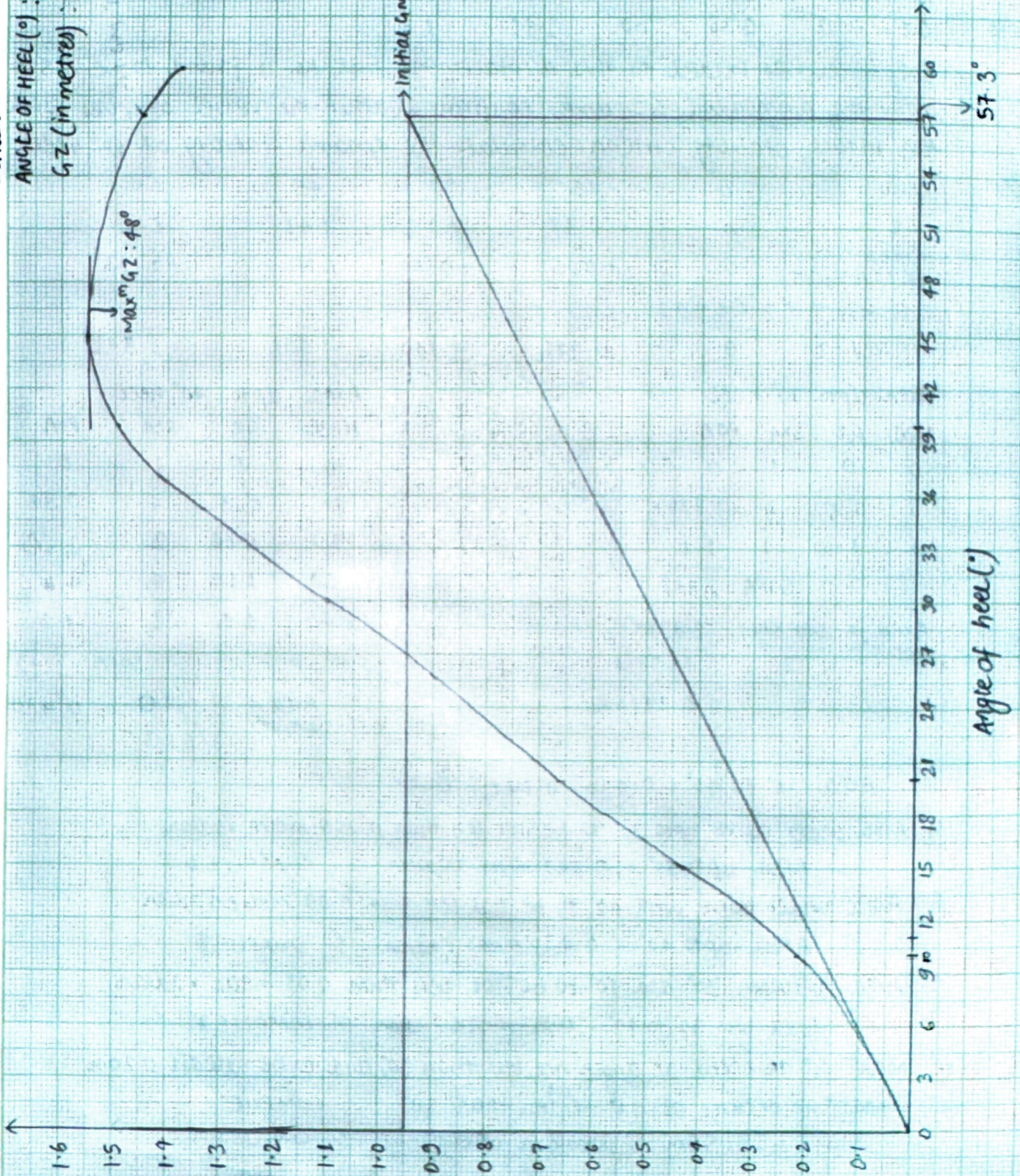
$$= 15060 \text{ mrt}$$

Ans

SCALE:

ANGLE OF HEEL ( $^{\circ}$ ) : 1 cm =  $3^{\circ}$

GZ (in metres) : 1 cm = 0.1 mtr.



JAN 2025  
APR 2024  
JULY 2023 P-2

A ship with light displacement 1700 t,  $K_G$  3.5m loaded with 1800t of cargo at  $K_G$  3.8m,  $K_M$  after loading is 3.8m while  $K_N$  values are as follows.

| Displacement (tonnes) | 10°  | 20°  | 30°  | 40°  | 60°  | 75°  |
|-----------------------|------|------|------|------|------|------|
| 3,000                 | 0.75 | 1.50 | 2.16 | 2.84 | 3.19 | 3.26 |
| 4,000                 | 0.77 | 1.54 | 2.30 | 2.92 | 3.25 | 3.26 |

Plot the GZ curve & show if the ship complies with IMO stability criteria

Soln:-

| HEEL                                     | 0 | 10    | 20    | 30    | 40    | 60    | 75     |
|------------------------------------------|---|-------|-------|-------|-------|-------|--------|
| $K_N$ @ 3000t                            | 0 | 0.75  | 1.50  | 2.16  | 2.84  | 3.19  | 3.26   |
| $K_N$ @ 4000t                            | 0 | 0.77  | 1.54  | 2.30  | 2.92  | 3.25  | 3.26   |
| So, $K_N$ values at 1700+1800 = 3500t    | 0 | 0.76  | 1.52  | 2.23  | 2.88  | 3.22  | 3.26   |
| (-) $K_G \sin \theta$ (USE Final $K_G$ ) | 0 | 0.635 | 1.250 | 1.827 | 2.349 | 3.164 | 3.529  |
| GZ                                       | 0 | 0.125 | 0.270 | 0.403 | 0.531 | 0.056 | -0.269 |

To find final  $K_G$

| Remarks | W        | $K_G$ | v. moment |
|---------|----------|-------|-----------|
| Initial | 1700     | 3.5   | 5950      |
| Loaded  | (+) 1800 | 3.8   | (+) 6840  |

Final w : 3500

Final v. moment : 12790

$$\text{Final } K_G = \frac{\text{Final v. moment}}{\text{Final w}} = \frac{12790}{3500} = 3.654 \text{ m}$$

PLOT THE GZ CURVE

| AREA UPTO 30° HEEL |       |    |       |
|--------------------|-------|----|-------|
| HEEL               | GZ    | SM | POA   |
| 0                  | 0     | 1  | 0     |
| 10                 | 0.125 | 3  | 0.375 |
| 20                 | 0.270 | 3  | 0.810 |
| 30                 | 0.403 | 1  | 0.403 |

SOPA: 1.588

$$\text{Area} = \frac{\text{SOPA} \times 3h}{8} = \frac{1.588 \times 3 \times 10}{8 \times 57.3}$$

$$= 5.955 \text{ m}^2$$

$$= 0.104 \text{ metre radian}$$

| AREA UPTO 40° HEEL |       |    |       |
|--------------------|-------|----|-------|
| HEEL               | GZ    | SM | POA   |
| 0                  | 0     | 1  | 0     |
| 10                 | 0.125 | 4  | 0.5   |
| 20                 | 0.270 | 2  | 0.54  |
| 30                 | 0.403 | 4  | 1.612 |
| 40                 | 0.531 | 1  | 0.531 |

SOPA: 3.183

$$\text{Area} = \frac{\text{SOPA} \times h}{3} = \frac{3.183 \times 10}{3 \times 57.3} = 0.185 \text{ m}^2$$

$$\begin{aligned}\text{Area between } 30^\circ \text{ to } 40^\circ &= 0.185 - 0.104 \\ &= 0.081 \text{ metre radian}\end{aligned}$$

(A) Area under curve upto  $30^\circ$  to be not less than 0.055 metre radian

Area upto  $30^\circ = 0.104$  metre radian : COMPLIED

(B) Area under curve upto  $40^\circ$  to be not less than 0.09 metre radian

Area upto  $40^\circ = 0.185$  metre radian : COMPLIED

(C) Area between  $30^\circ$  &  $40^\circ$  to be not less than 0.03 metre radian

Area b/w  $30^\circ$  to  $40^\circ = 0.081$  metre radian : COMPLIED

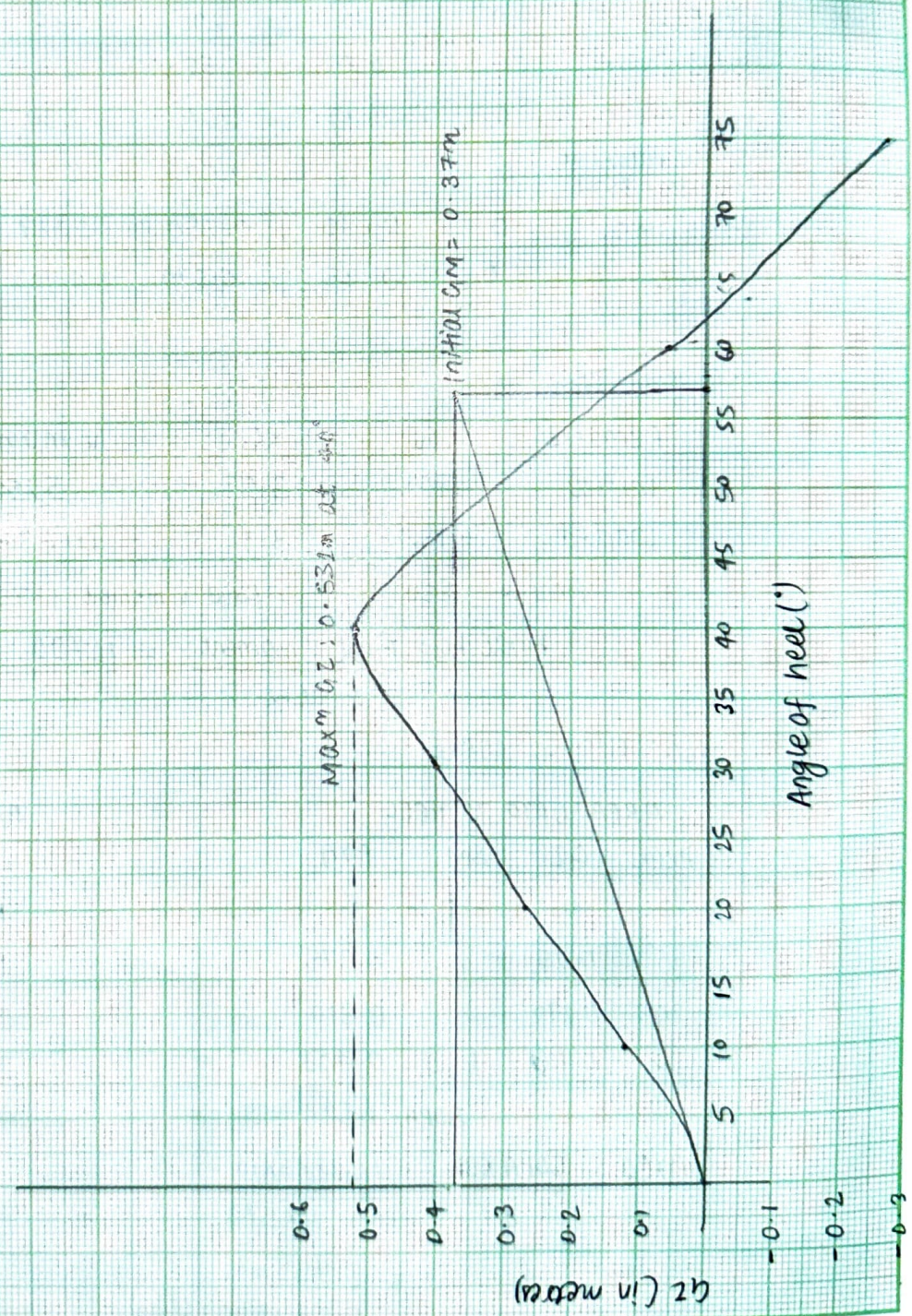
(E) Max<sup>m</sup> GZ to occur at angle not less than  $30^\circ$ , and to be atleast 0.20m

Max<sup>m</sup> GZ occur at  $40^\circ$  } COMPLIED  
Max<sup>m</sup> GZ : 0.531m

(F) Initial GM to be not less than 0.15m

Initial GM : 0.37m : COMPLIED

SCALE:  
 ANGLE OF HEEL ( $^{\circ}$ ) : 1cm = 5"  
 GZ (in metres) : 1cm = 0.1 metre



JULY 2022 M.V HINDSHIP arrives in Condition No. 7. Shore crane is used to discharge the deck cargo of locomotives that was loaded 4m off the CL to Port. By use of curve of statical stability, calculate the list caused when the deck cargo of locomotive is lifted to the shore crane

Soln:-  
Initial displacement : 18529.3 t  
Locomotive : (-) 760.0 t  
Final displacement : 17769.3 t

| Remarks | W       | K <sub>G</sub>          | v. moment |
|---------|---------|-------------------------|-----------|
| 18529.3 | 18529.3 | 7.807                   | 144653    |
| (-) 760 | (-) 760 | 13.83                   | (-) 10510 |
| 17769.3 | 17769.3 | Final v. moment: 134143 |           |

$$\text{Final } K_G = \frac{\text{Final v. moment}}{\text{Final } W} = \frac{134143}{17769.3} = 7.549 \text{ m}$$

$$K_G : 7.549 \text{ m}$$

$$\text{FSC} : (+) 0.087 \text{ m} \quad \left( \frac{\text{FSM}}{W} = \frac{1552}{17769.3} \right)$$

$$\text{Corrected } K_G : 7.636 \text{ m}$$

$$G_G = \frac{W \times d}{W} \quad \left( \frac{\text{FSM}}{W} = \frac{1552}{17769.3} \right)$$

$$= \frac{760 \times 4}{17769.3}$$

$$= 0.171 \text{ m}$$

| Heel                  | 0      | 5     | 10    | 15    | 20    | 25    | 30    | 40    |
|-----------------------|--------|-------|-------|-------|-------|-------|-------|-------|
| KN                    | 0.0    | 0.756 | 1.507 | 2.240 | 2.987 | 3.653 | 4.338 | 5.560 |
| -K <sub>G</sub> sin θ | 0      | 0.666 | 1.326 | 1.976 | 2.612 | 3.227 | 3.818 | 4.908 |
| GZ                    | 0      | 0.090 | 0.181 | 0.264 | 0.375 | 0.426 | 0.520 | 0.652 |
| -G <sub>G</sub> cos θ | 0.171  | 0.170 | 0.168 | 0.165 | 0.161 | 0.155 | 0.148 | 0.131 |
| Corrected GZ          | -0.171 | -0.08 | 0.013 | 0.099 | 0.214 | 0.271 | 0.372 | 0.521 |

PLOT GZ CURVE

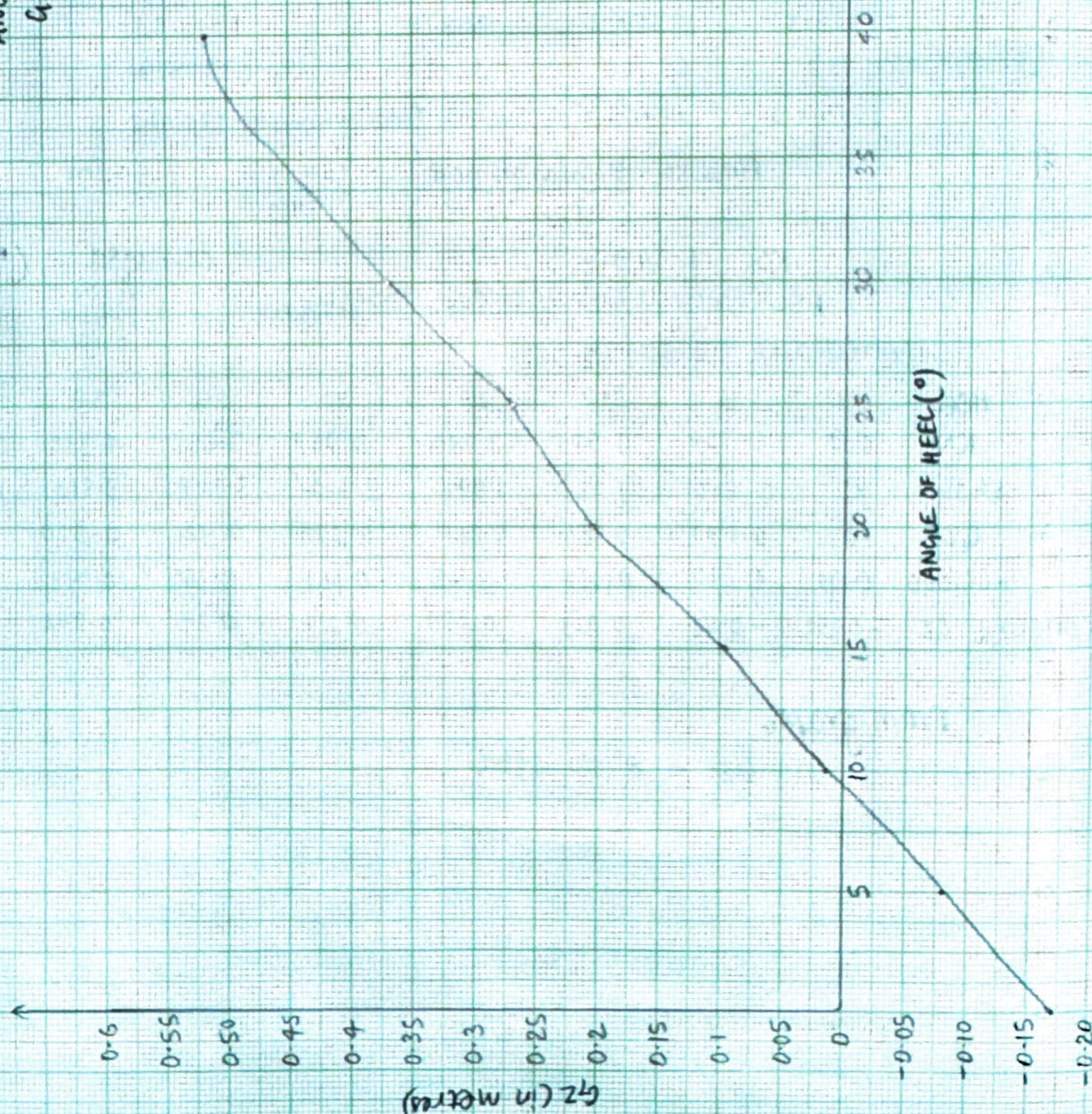
From graph,

$$\text{List} = 8^\circ \text{ to stbd}$$

SCALE:

ANGLE OF HEEL ( $^{\circ}$ ): 20m = 5"

GZ (in metres): 1cm = 0.05mtr



practice sum M.v Hindship displacement 19,200t has 300t of cargo to shift horizontally by 7 metre & vertically downward by 4m. Draw the GZ curve & calculate the list & confirm that vessel complies with IMO stability criteria. (FSM=2000, KG: 7.2m)

| SOL:- | Remarks | W     | KG  | V. moment |
|-------|---------|-------|-----|-----------|
|       | 19200   | 19200 | 7.2 | 138240    |
|       | Shift   | 300   | 4   | (-) 1200  |
|       |         | 19200 |     | 137040    |

$$\text{Final } KG = \frac{\text{Final V. moment}}{\text{Final W}} = \frac{137040}{19200} = 7.1375 \text{ m}$$

$$KG: 7.1375$$

$$FSC: (+) 0.1040 \quad (2000/19200 = 0.104)$$

$$\text{Corrected } KG: 7.242 \text{ m}$$

$$G_{G1} = \frac{W \times d}{W} = \frac{300 \times 7}{19200} = 0.109$$

| Heel                      | 0      | 5     | 10    | 15    | 20    | 25    | 30    | 40    | 45    | 60    |
|---------------------------|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| KN                        | 0      | 0.766 | 1.530 | 2.263 | 2.982 | 3.608 | 4.288 | 5.444 | 5.924 | 6.976 |
| corrected KG sine         | 0      | 0.631 | 1.258 | 1.874 | 2.477 | 3.061 | 3.621 | 4.655 | 5.121 | 6.272 |
| GZ                        | 0      | 0.135 | 0.272 | 0.389 | 0.505 | 0.547 | 0.667 | 0.789 | 0.803 | 0.704 |
| - * G <sub>G1</sub> cos θ | 0.109  | 0.109 | 0.107 | 0.105 | 0.102 | 0.099 | 0.094 | 0.083 | 0.077 | 0.055 |
| corrected GZ              | -0.109 | 0.026 | 0.165 | 0.284 | 0.403 | 0.448 | 0.573 | 0.706 | 0.726 | 0.649 |

PLOT THE GZ CURVE

From GZ curve, List = 4°

| Area upto 30° HEEL                                                                 |        |    |        |
|------------------------------------------------------------------------------------|--------|----|--------|
| Heel                                                                               | GZ     | SM | POA    |
| 0                                                                                  | -0.109 | 1  | -0.109 |
| 10                                                                                 | 0.165  | 3  | 0.495  |
| 20                                                                                 | 0.403  | 3  | 1.209  |
| 30                                                                                 | 0.573  | 1  | 0.573  |
| SOPA = 2.168                                                                       |        |    |        |
| Area = $\frac{SOPA \times 3h}{8} = \frac{2.168 \times 3 \times 10}{8 \times 57.3}$ |        |    |        |

$$= 8.13 \text{ m}^2$$

$$= 0.142 \text{ m/r}$$

| AREA UPTO 40° HEEL |        |    |        |
|--------------------|--------|----|--------|
| Heel               | GZ     | SM | POA    |
| 0                  | -0.109 | 1  | -0.109 |
| 10                 | 0.165  | 4  | 0.66   |
| 20                 | 0.403  | 2  | 0.806  |
| 30                 | 0.573  | 4  | 2.292  |
| 40                 | 0.706  | 1  | 0.706  |
| SOPA = 4.355       |        |    |        |

$$\text{Area} = \frac{SOPA \times h}{3} = \frac{4.355 \times 10}{3 \times 57.3}$$

$$= 0.253 \text{ m/r}$$

$$\text{Area between } 30^\circ \text{ to } 40^\circ = 0.253 - 0.142 \\ = 0.111 \text{ meter radian}$$

Ⓐ Area under curve upto  $30^\circ$  to be not less than 0.055 meter radian  
Area upto  $30^\circ = 0.142$  meter radian : COMPLIED

Ⓑ Area under curve upto  $40^\circ$  to be not less than 0.09 meter radian  
Area upto  $40^\circ = 0.253$  meter radian : COMPLIED

Ⓒ Area between  $30^\circ$  &  $40^\circ$  to be not less than 0.03 meter radian  
Area between  $30^\circ$  to  $40^\circ = 0.111$  meter radian : COMPLIED

Ⓔ Max<sup>m</sup> GZ to occur at angle not less than  $30^\circ$ , and to be atleast 0.20m.  
 $\left. \begin{array}{l} \text{Max}^m \text{ GZ occur at } 48^\circ \\ \text{Max}^m \text{ GZ} = 0.73\text{m} \end{array} \right\} \text{COMPLIED}$

Ⓕ Initial GM to be not less than 0.15m

At zero, value of GZ is negative  
degree heel

So, we will find GM by calculation

$$KM @ 19200t : 8.400\text{m}$$

$$KA : 7.242\text{m}$$

$$GM(F) : 1.158\text{m}$$

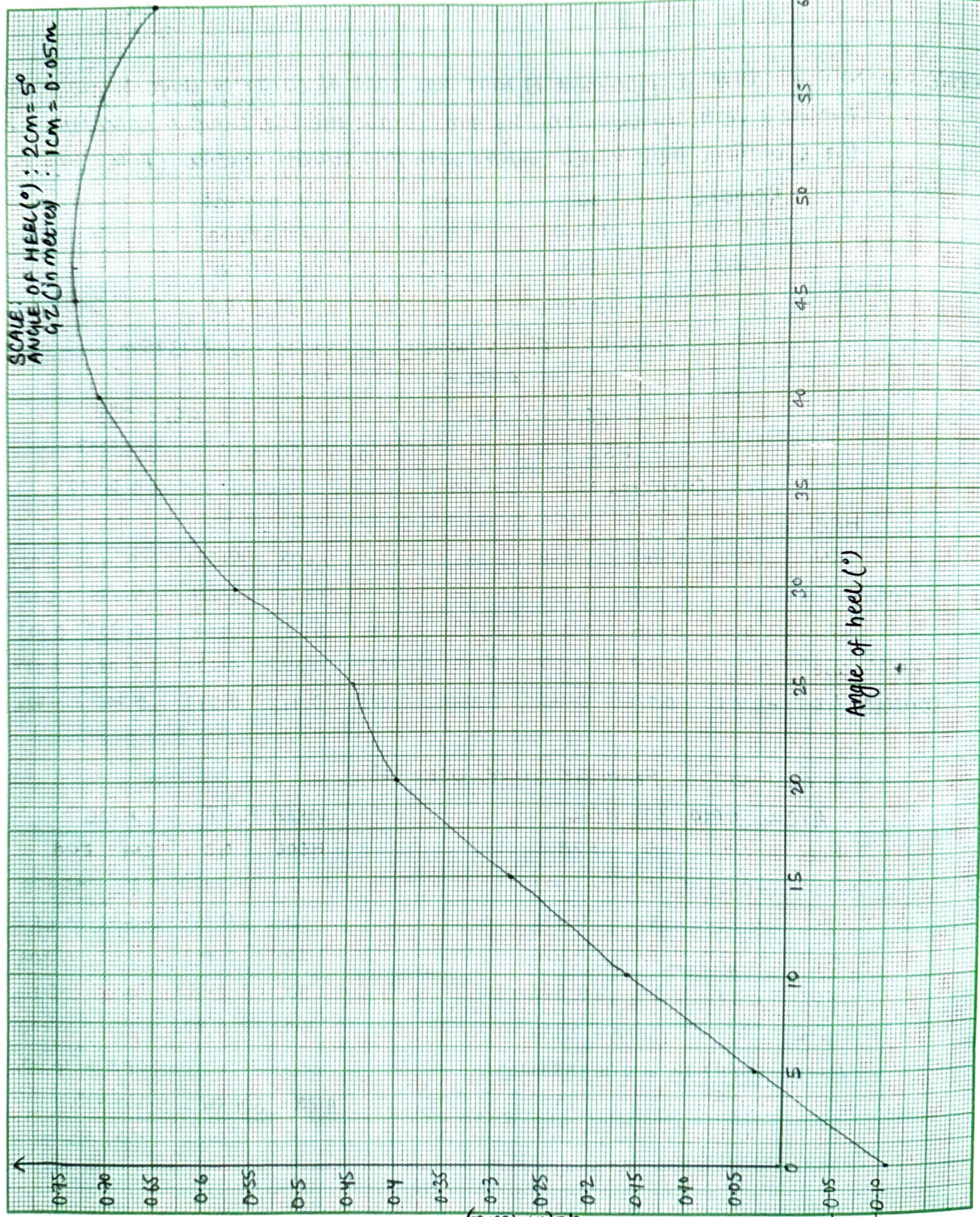


i.e. not less than 0.15m : COMPLIED

$$19051 \quad 8.388$$

$$19537 \quad 8.428$$

$$\frac{0.04}{486} \times 149 =$$



OCT 2023  
PAPER 2  
JULY 2022

A ship in upright conditions, having displacement 15000t and KG 7.0m, FSM 400tm, following GZ value were obtained:

|           |   |      |     |      |     |
|-----------|---|------|-----|------|-----|
| Heel(deg) | 0 | 15   | 30  | 45   | 60  |
| GZ(m)     | 0 | 0.38 | 1.0 | 1.41 | 1.2 |

Vessel now take 200t of ballast in top side tank, Kg 9.0m and 5.0m to port of centerline. FSM in final condition is 900tm. If the KN values remain unchanged after ballasting. Calculate the resultant list with the help of statical stability curve

Soln:-

| Remarks   | W      | KG  | v.moment               |
|-----------|--------|-----|------------------------|
| Initial   | 15000  | 7.0 | 105000                 |
| Ballast   | (+)200 | 9.0 | (+) 1800               |
| Final W : | 15200  |     | Final v.moment: 106800 |

$$\text{Final } K_G = \frac{\text{Final v.moment}}{\text{Final W}}$$

$$= \frac{106800}{15200} = 7.026 \text{ m}$$

$$\text{FSC} = \text{FSM}/W = 900/15200 = 0.059 \text{ m}$$

$$\text{Corrected } K_G = 7.085 \text{ m}$$

For vertical shift up :  $-G_G \sin \theta$

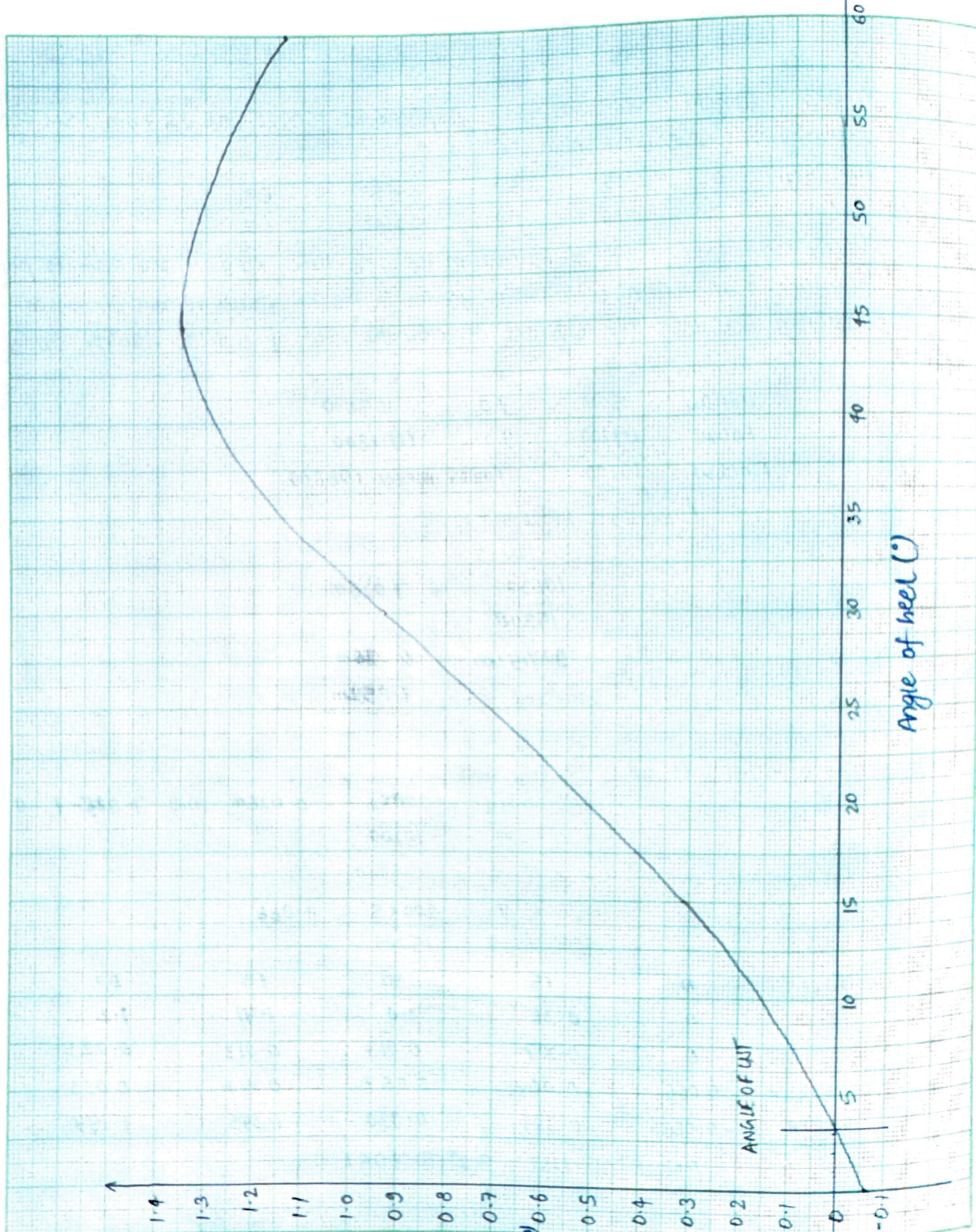
$$G_G = \frac{W \times d}{W} = \frac{200 \times 2}{15200} = 0.026 \text{ m (OR)} 7.085 - 7 = 0.085 \text{ m}$$

For horizontal ship :  $-G_G \cos \theta$

$$G_G = \frac{W \times d}{W} = \frac{200 \times 5}{15200} = 0.066$$

|                    |        |       |       |       |       |
|--------------------|--------|-------|-------|-------|-------|
| Heel               | 0      | 15    | 30    | 45    | 60    |
| GZ                 | 0      | 0.38  | 1.0   | 1.41  | 1.2   |
| $-G_G \sin \theta$ | 0      | 0.007 | 0.013 | 0.018 | 0.023 |
| $-G_G \cos \theta$ | 0.066  | 0.064 | 0.057 | 0.047 | 0.033 |
| Corrected GZ       | -0.066 | 0.309 | 0.930 | 1.345 | 1.144 |

ANGLE OF LIST :  $3.2^\circ$  TO PORT



GZ  
(in meter)